

High Precision Measurements

$$\text{of } R = \sigma_L / \sigma_\pi$$

in the Nucleon Resonance  
Region

M. Eric Christy

Hampton University

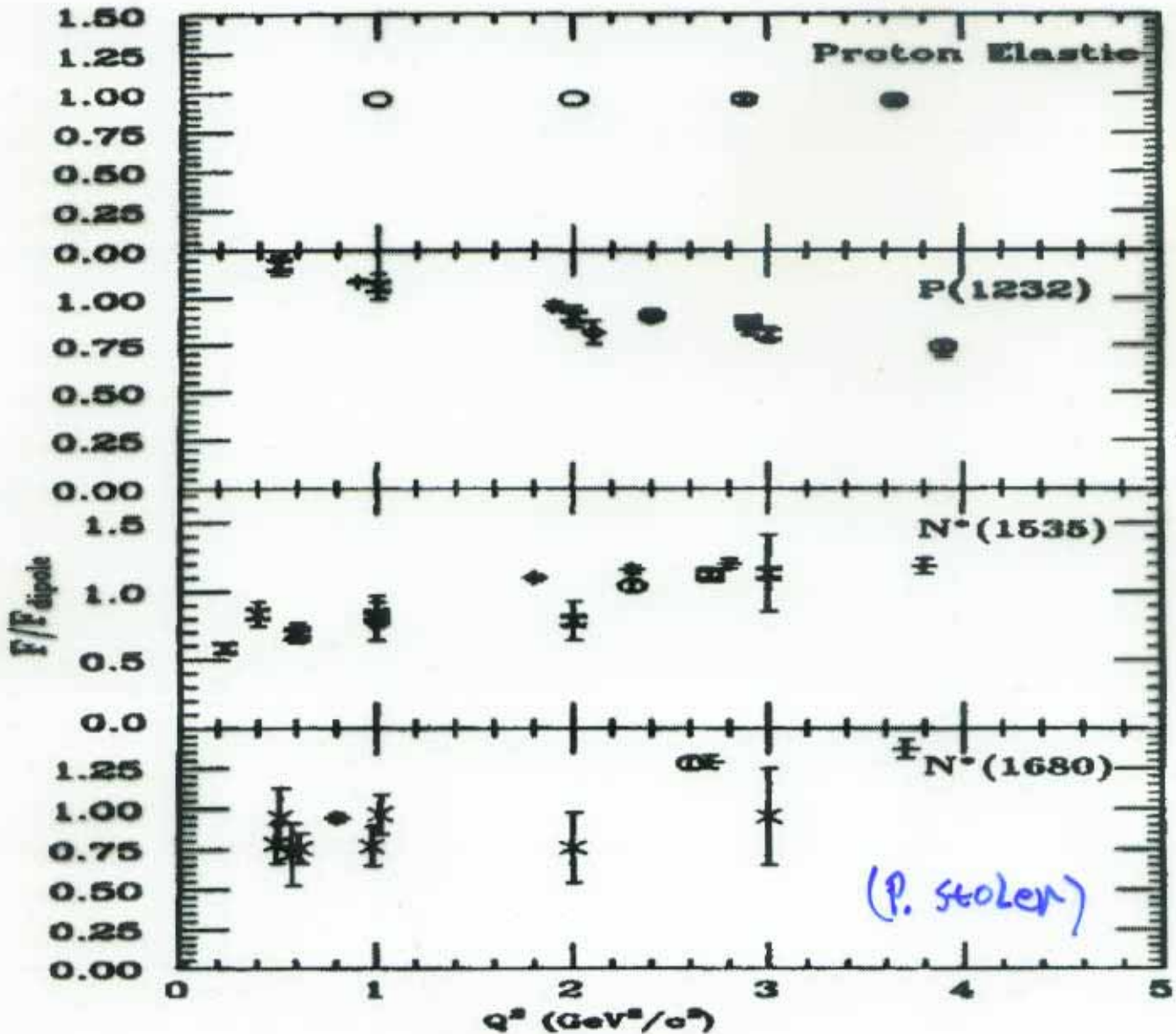
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E94-110

# Resonant Transition Form Factors

$$|F_{\Delta}(Q^2)|^2 = \frac{2\Gamma_R \pi M_{\Delta}}{Q^2} F_1$$

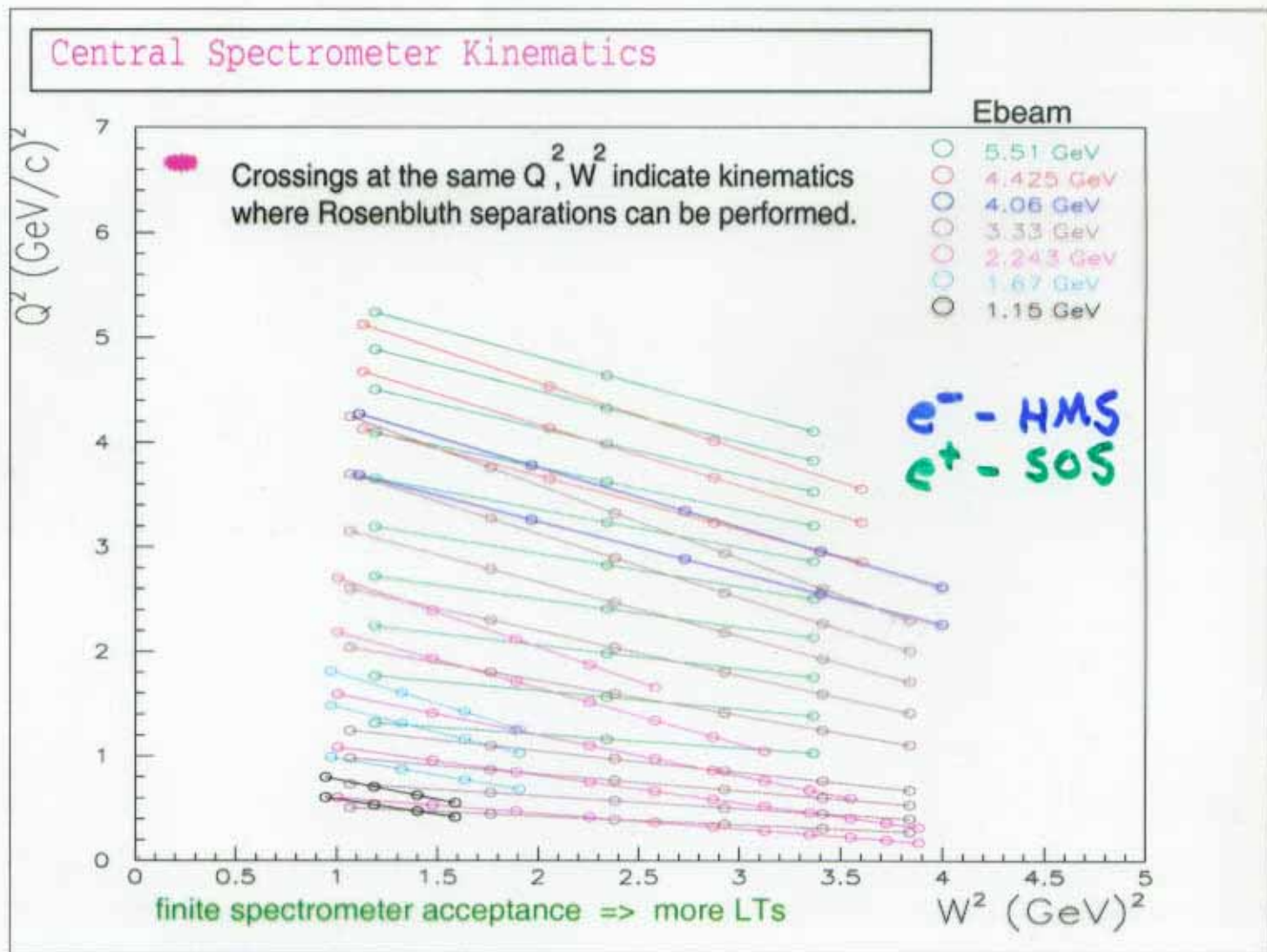
$$\propto \frac{A_{1/2}^2 + A_{3/2}^2}{Q^2}$$



Assumes  $\sigma_L^{\text{res}} = 0$  for inclusive extraction

# E94-110 Central Spectrometer Kinematics

Essentially the same as PR02-009



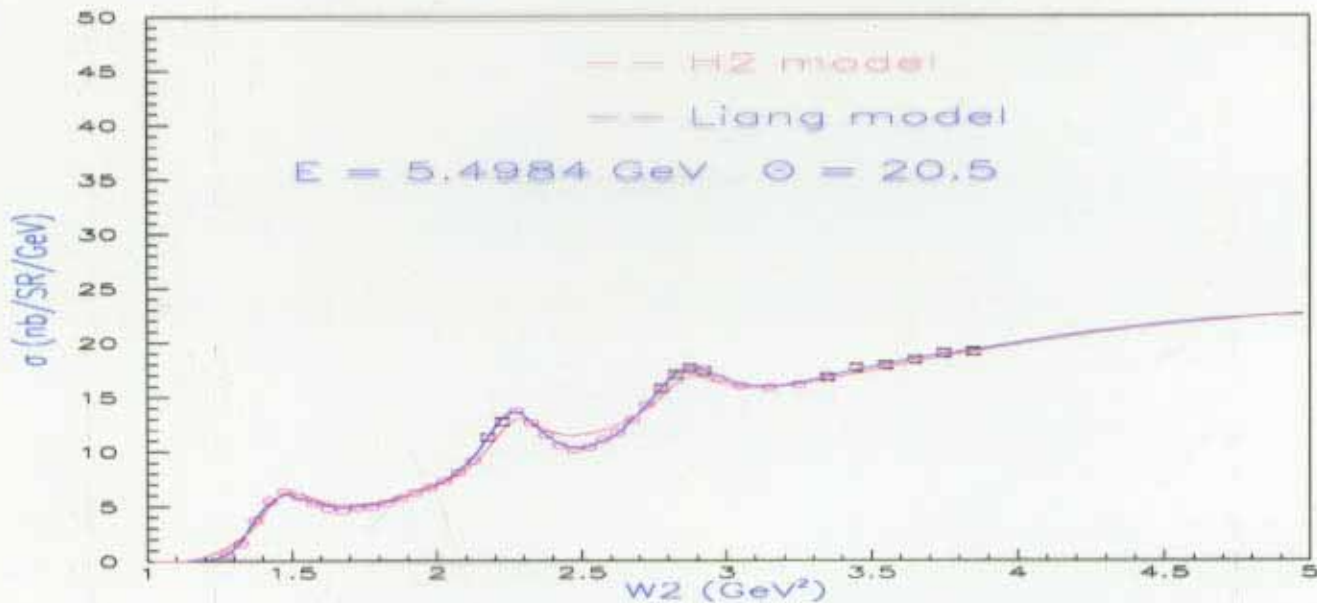
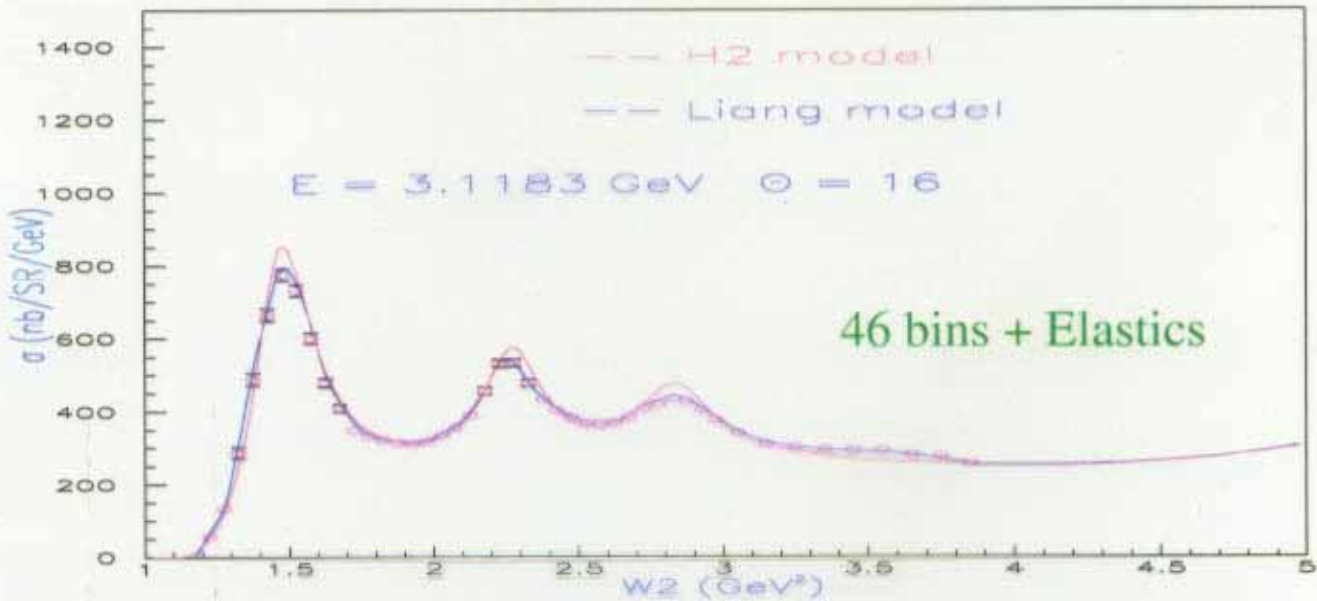
2 Methods are employed for extracting the complete unpolarized structure functions:

1. Rosenbluth separations where possible.  
(Some kinematic evolution is needed)
2. Iteratively Fit to  $F_2$  and  $R$  over the entire kinematic range.



Global extracting

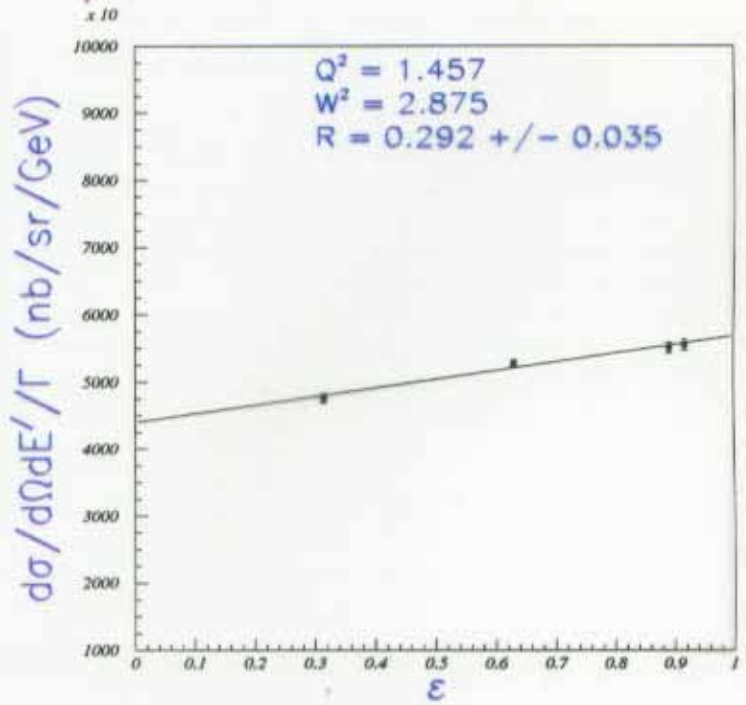
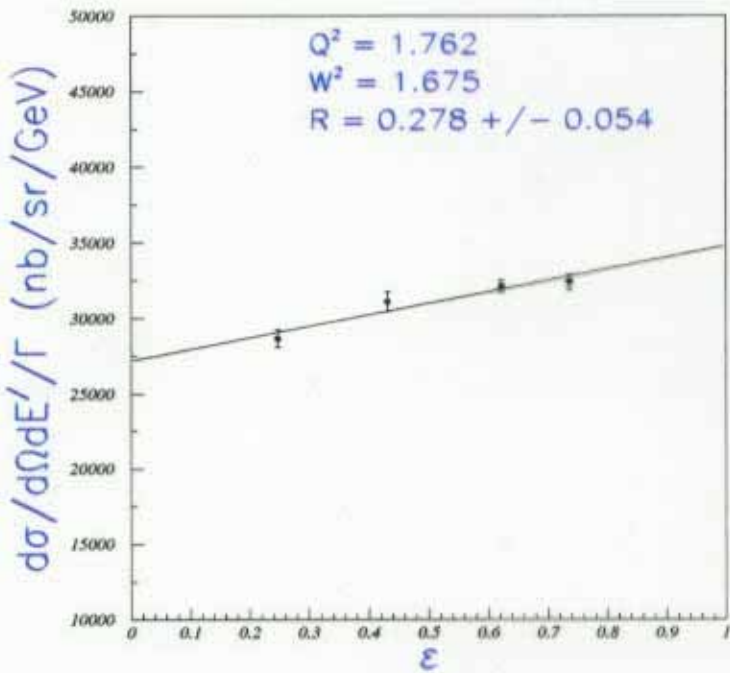
# E94-110 Cross Sections



- ➔ Statistical uncertainties are included (typically < 1 %) (overlapping points are averaged).
- ➔ Current fit (Liang) reproduces data cross section well.

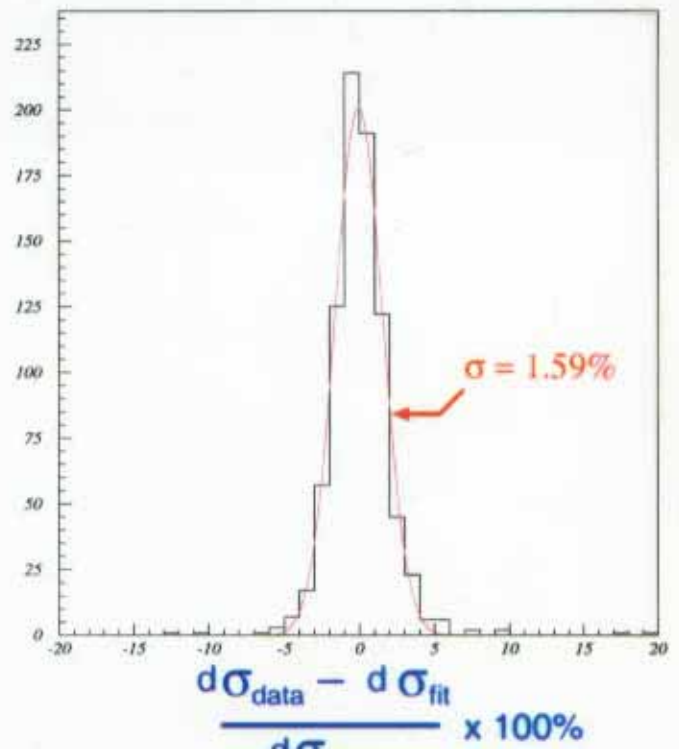
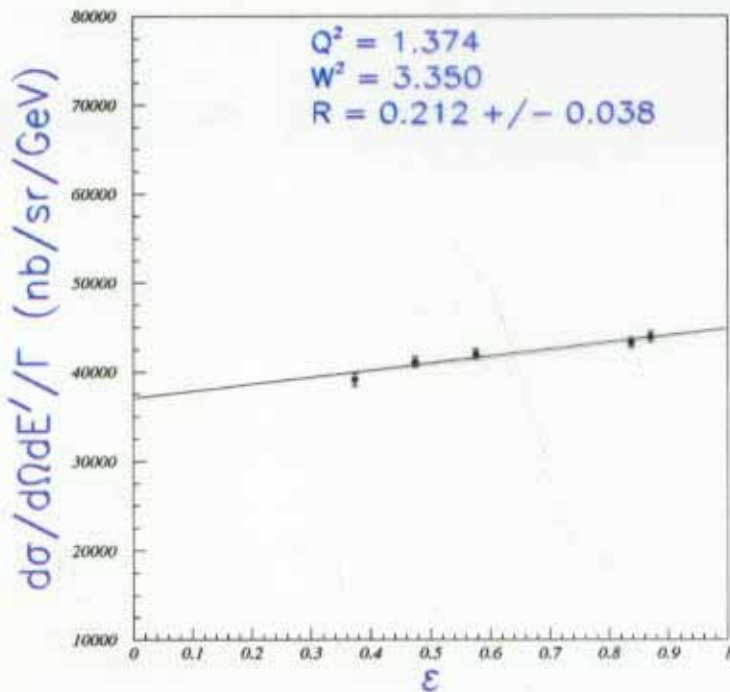
# L/T Separations

180+ Direct L/T Separations Performed



$$\frac{1}{\Gamma} \frac{d\sigma}{d\Omega dE} = [\sigma_T(W^2, Q^2) + \epsilon \sigma_L(W^2, Q^2)]$$

1.0 - 1.5% pt-to-pt systematics



## Model Iteration Procedure

Model is used for radiative corrections and bin-centering the data in  $\theta$ .

Extract  $\sigma^{\text{exp}}$  from data.

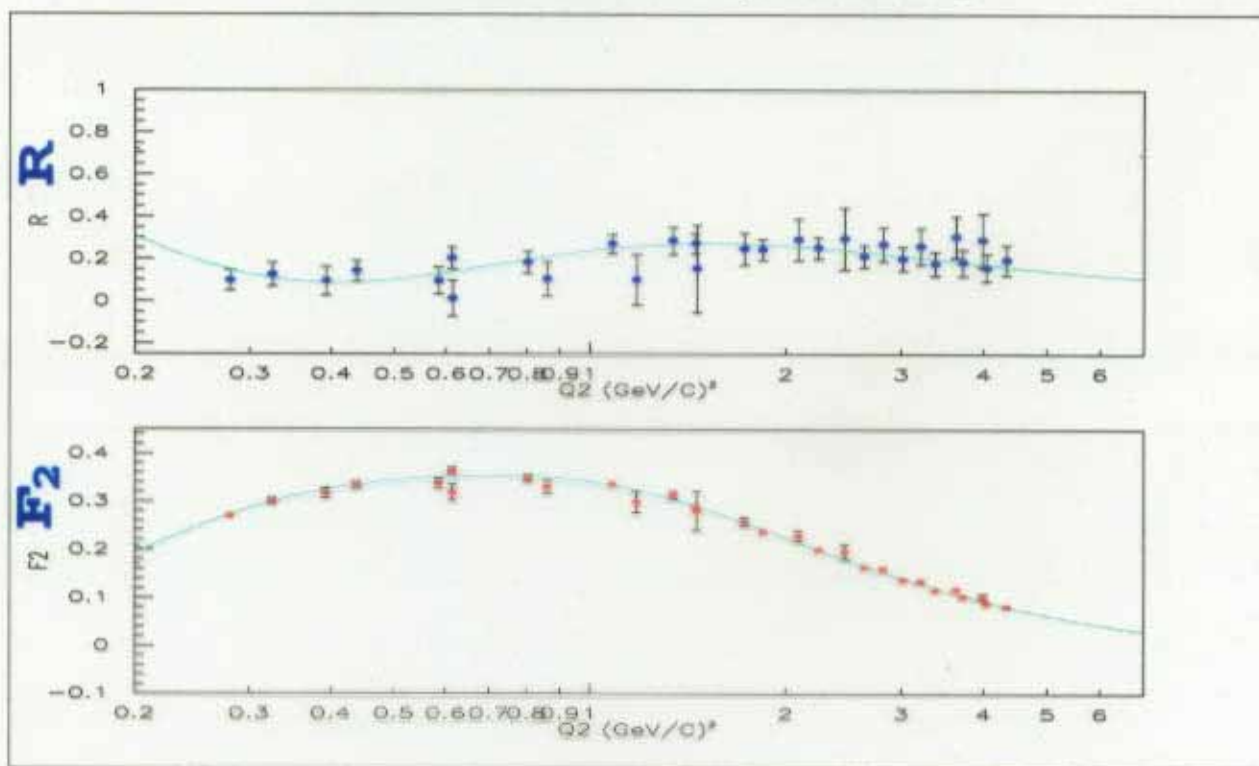
Use model to decompose  $\sigma^{\text{exp}}$  into  $F_2^{\text{exp}}$  and  $R^{\text{exp}}$ .

For each  $W^2$  bin, fit  $F_2^{\text{exp}}$  and  $R^{\text{exp}}$  vs  $Q^2$  to get new model.

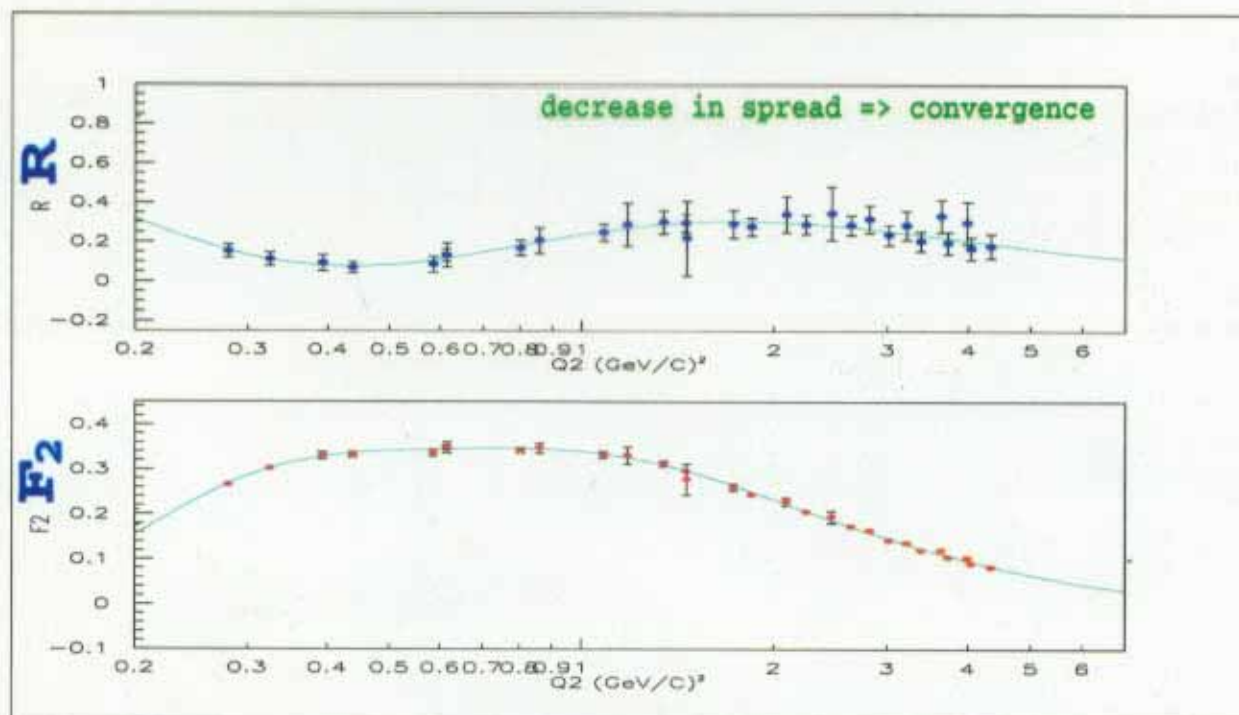
- Strength gets shuffled between  $F_2$  and  $R$  until convergence is reached.
- When calling model, interpolate in  $W^2$

# Structure Function Extraction via Model Iteration

3rd Resonance Peak, Iteration 0:



3rd Resonance Peak, Iteration 2:

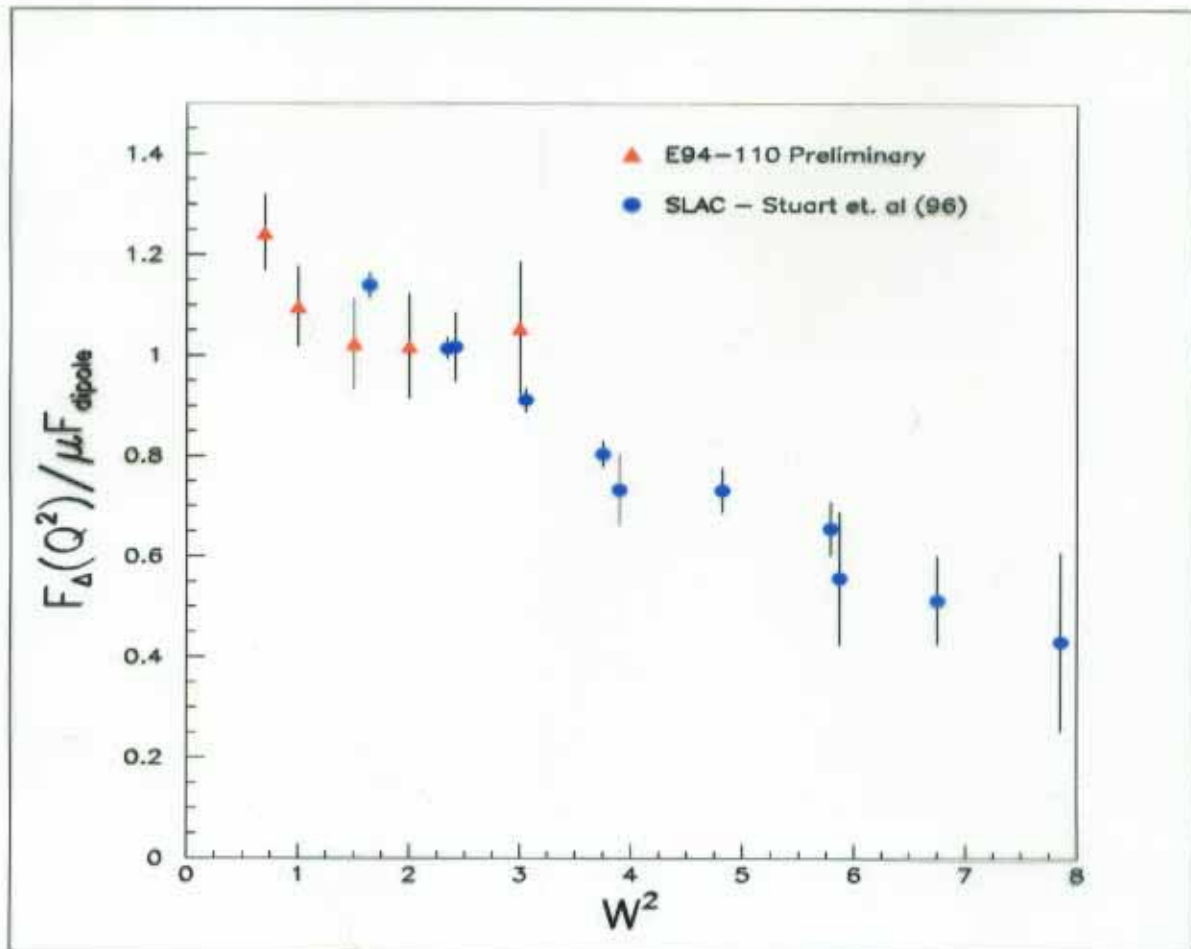


- First <sup>precision</sup> separation of  $\sigma_2 / \sigma_{\pi}$  in nucleon Resonance Region.
- Both  $\sigma_{\pi} + \sigma_2$  show Resonant structure ( $\sigma_2^{\text{res}} \neq 0$ )
- Lots of good physics
- \*  $F_1, F_2$  Moments at low  $Q^2$
  - \* Transition FFs
  - \* Quark-Hadron duality in  $L/\pi$  channels



## Resonant Transition Form Factors

$$\left| F_{\Delta}(Q^2) \right|^2 = \frac{2\Gamma_R \pi M_{\Delta}}{Q^2} F_1$$



Expect that  $\Delta$  T.F.F. will be consistent with earlier results.

since  $\sigma_L^{\text{RES}}$  is small.

But for 2nd and 3rd Resonance region  $\sigma_L^{\text{RES}}$  is not small!

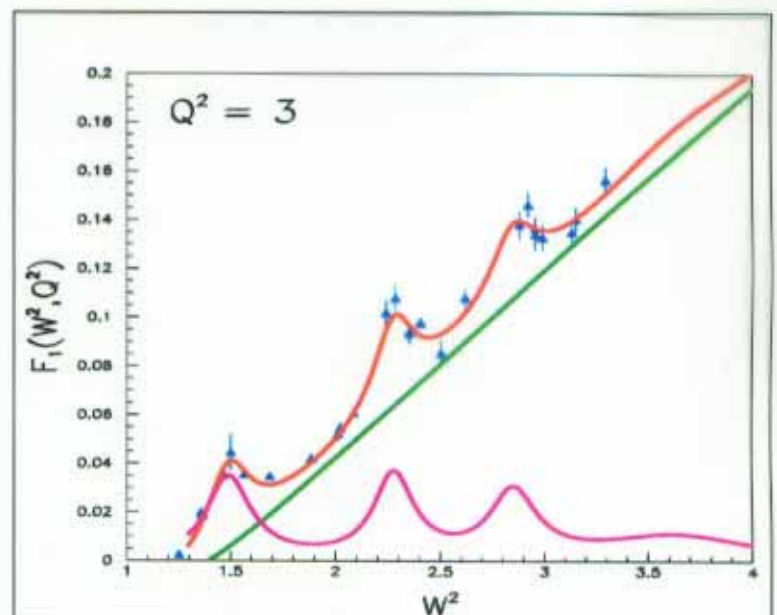
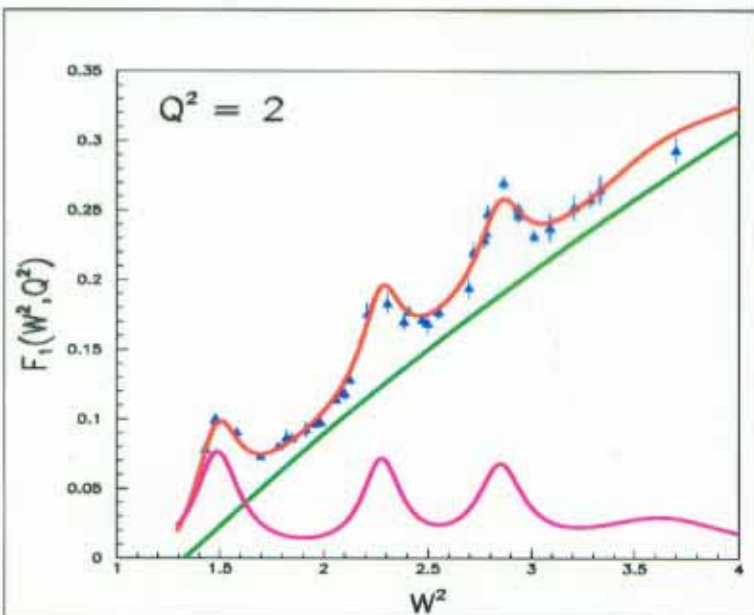
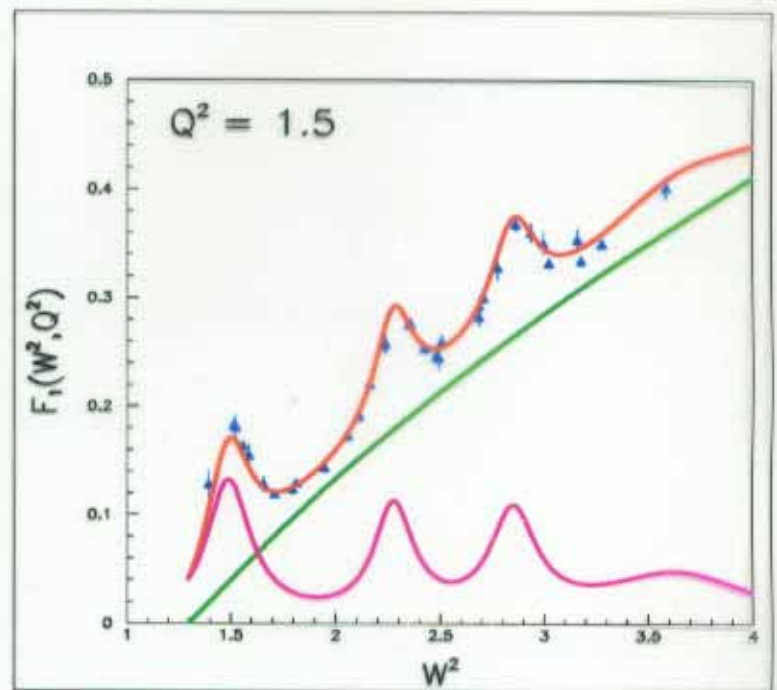
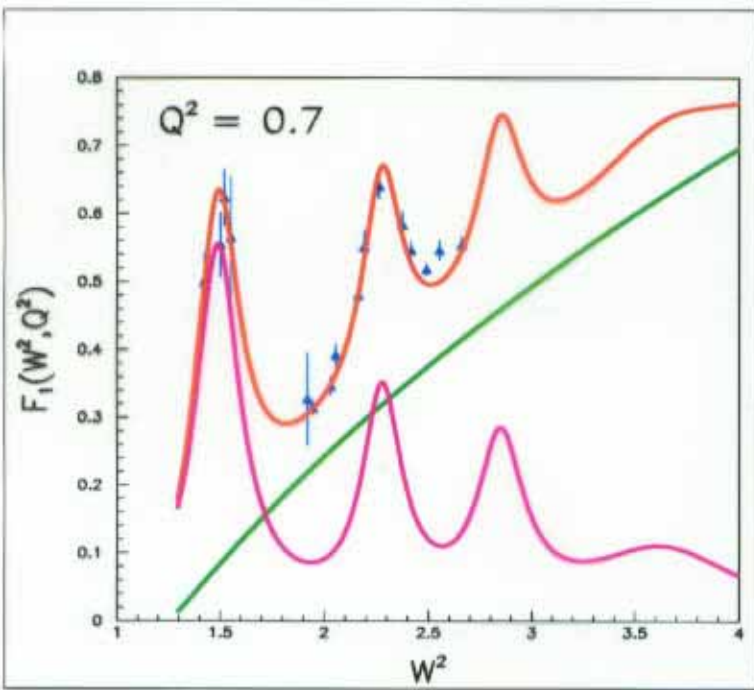
## Resonant Transverse Structure Function

$$\sigma_T = \frac{4\pi^2}{\kappa M_n} \alpha F_1$$

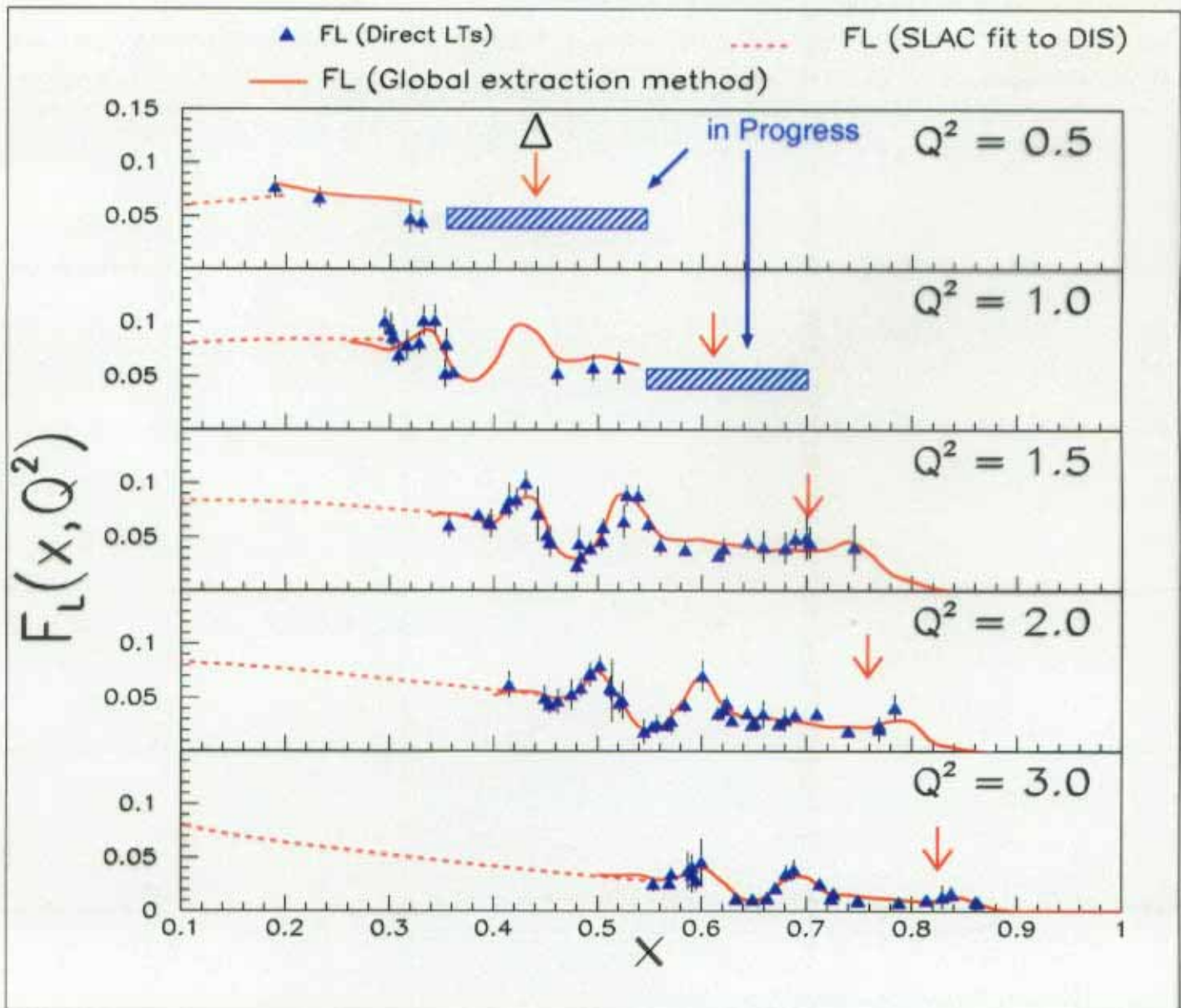
$$\kappa = \frac{W^2 - M_n^2}{2M_n}$$



Only 60% of Rosenbluth Separated data shown.  
10x as much cross section data to be included!



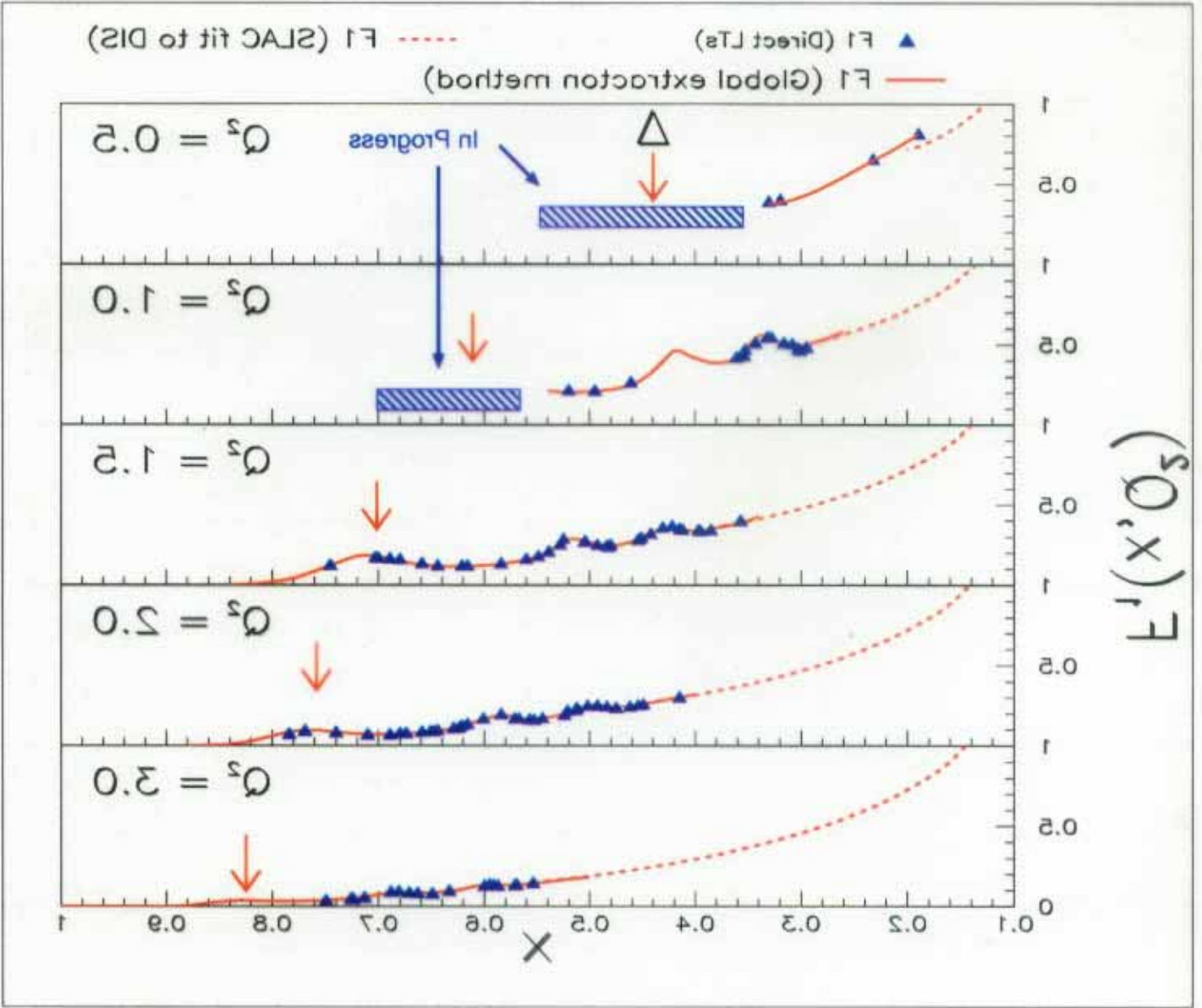
# Results for $F_L^p$



➡ Both longitudinal and transverse structure functions exhibit resonant behaviour

➡ Can easily extract moments, as all that is currently missing is resonance (large  $x$ ) data.

# Results for $F_1^p$



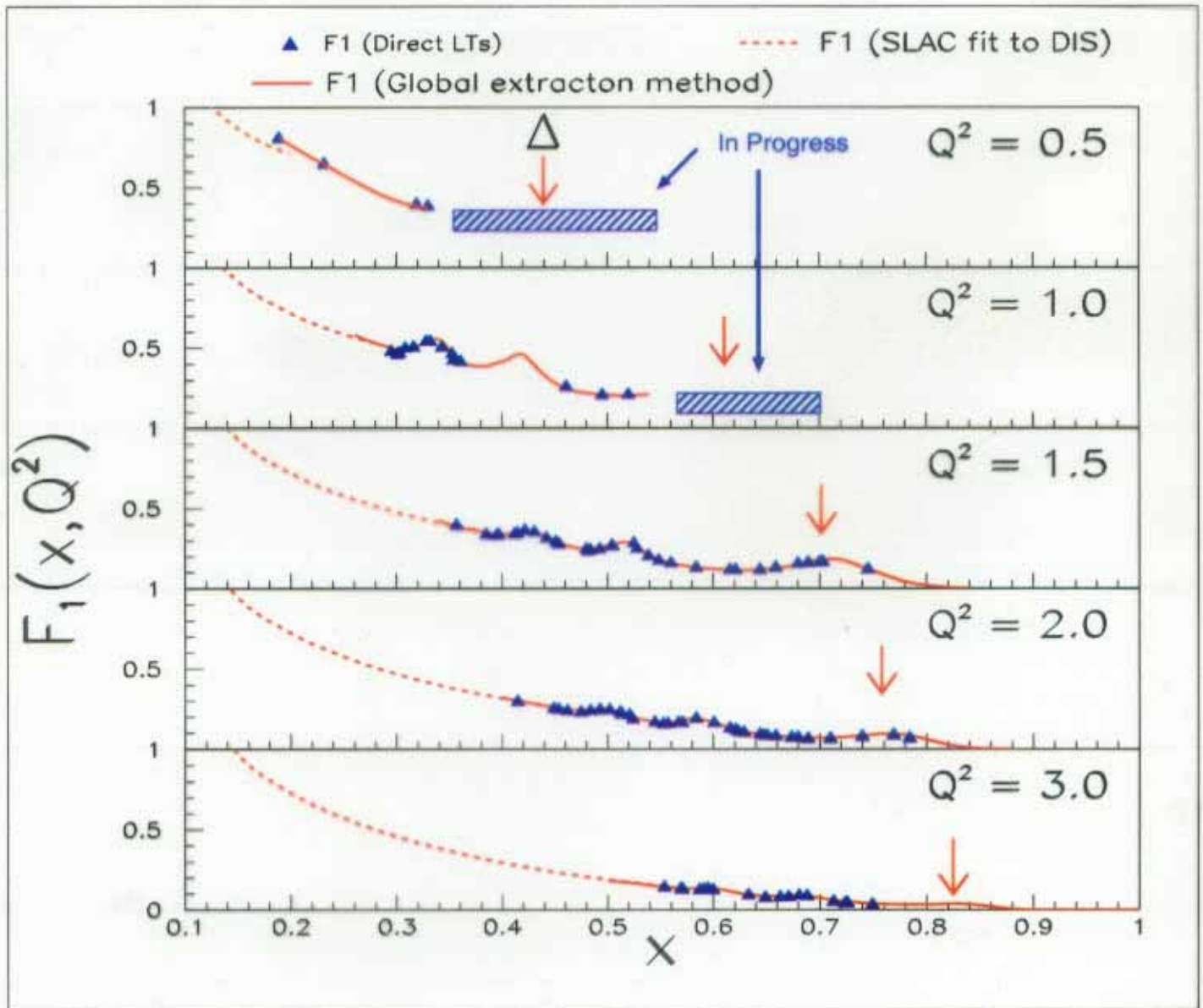
Publication in progress



Excellent agreement between global extraction and direct LTs

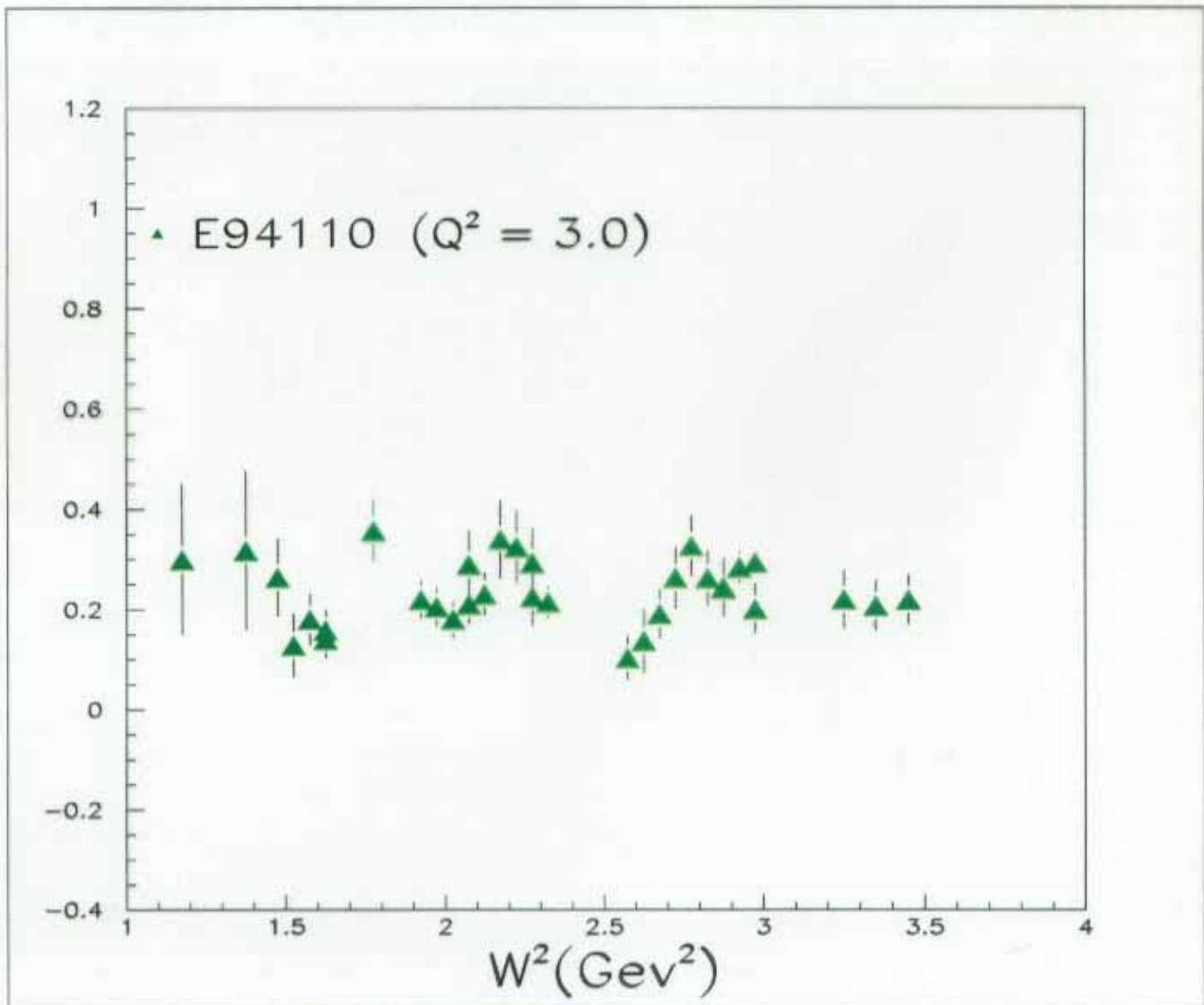


# Results for $F_1^p$



➡ Publication in progress

➡ Excellent agreement between global extraction and direct L-Ts

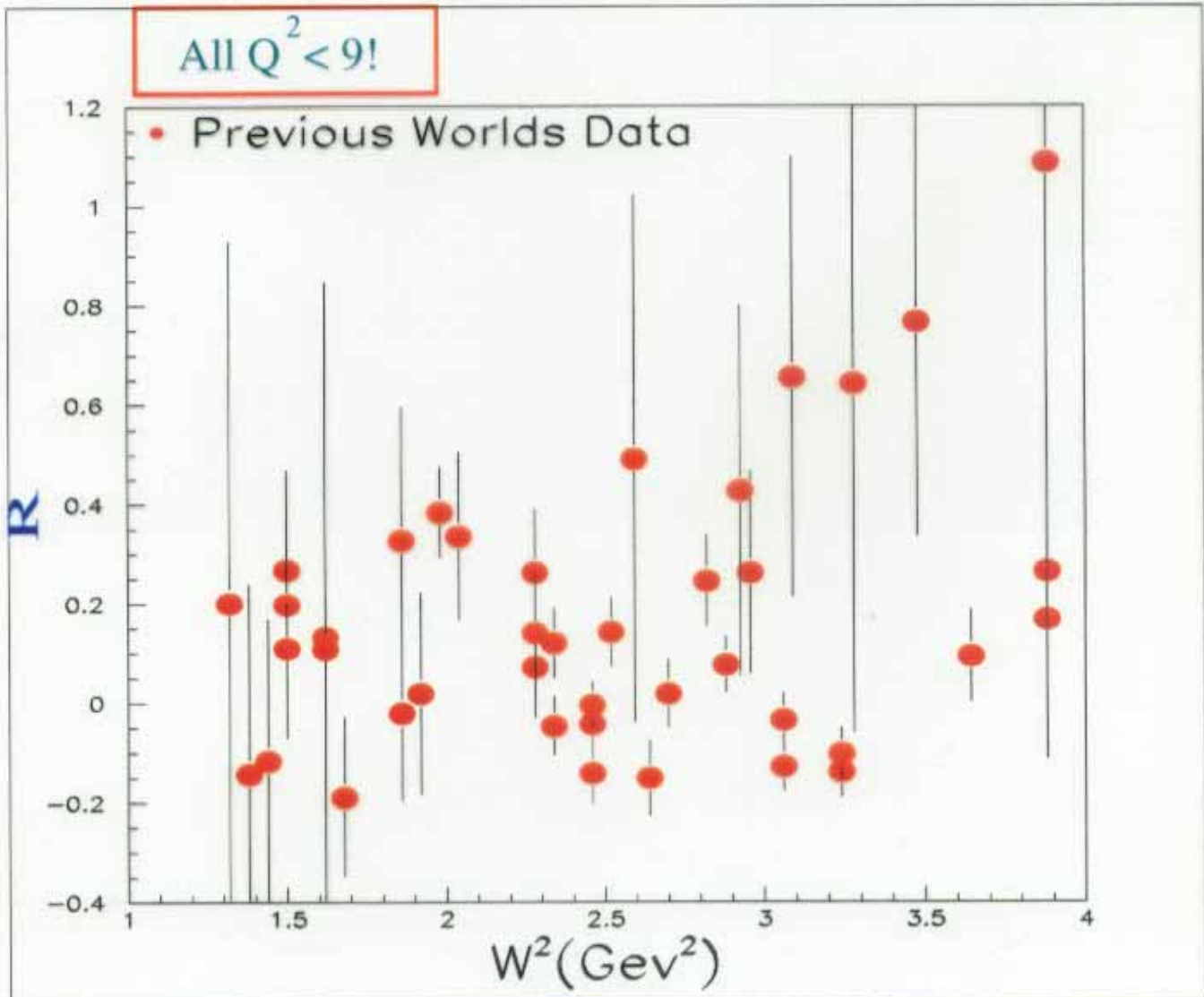


Comparable data will be obtained for the deuteron, where the L/T structure is even less well measured!

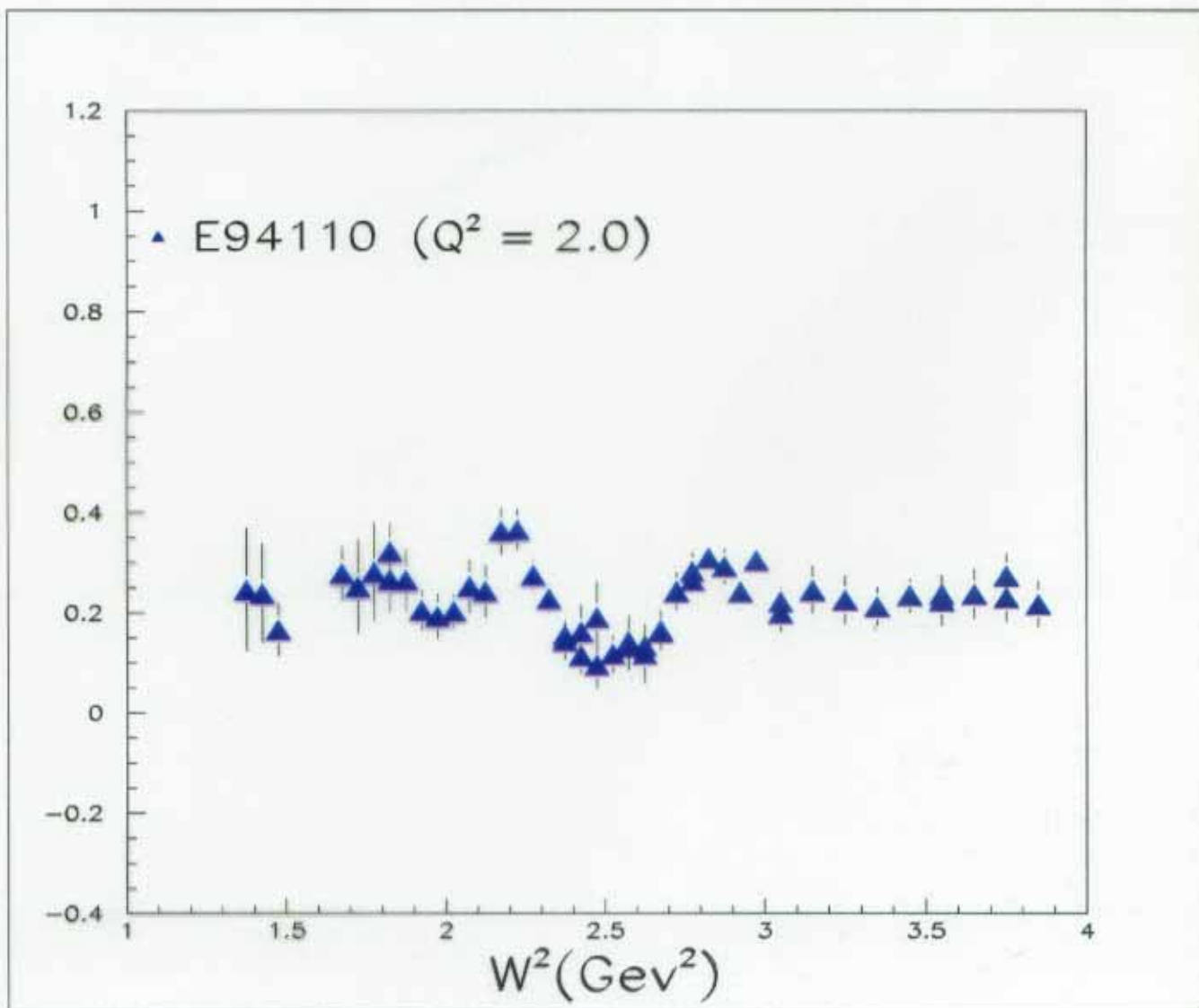
Both the  $W^2$  structure and the  $Q^2$  dependence can be studied!

# World's Data on Proton R in the Resonance Region

Prior to E94-110:



Prior: Could not explore Resonant Structure!  
(experiments optimized for DIS)



Comparable data will be obtained for the deuteron, where the L/T structure is even less well measured!



# Current Data on $R = \sigma_L / \sigma_T$ ( $F_L = 2xF_1 R$ )

Elastic

$$Q^2 < 8.83 \text{ GeV}^2/c^2$$

Resonance

$R = ?$

DIS

$$Q^2 < 50 \text{ GeV}^2/c^2$$

In NPM

for parton with intrinsic transverse momenta  $p_T$ :

$$R = \frac{2M}{Q} \frac{G_E(Q^2)}{G_M(Q^2)}$$

$$R = \frac{4(M^2 x^2 + \langle p_T^2 \rangle)}{Q^2 + \langle p_T^2 \rangle}$$

Charge - Current Structure of the Nucleon

(Higher twist effects from both kinematic (TM) and dynamic origins can significantly modify  $R$ .)

(At low  $x$ ,  $F_L$  is sensitive to the gluon distribution function.)

**Lacking data on  $R$  ( $F_L$ ) in Resonance Region**

Precise measurement of *complete* unpolarized structure functions in RR is needed for:

Gain further information about fundamental nucleon structure

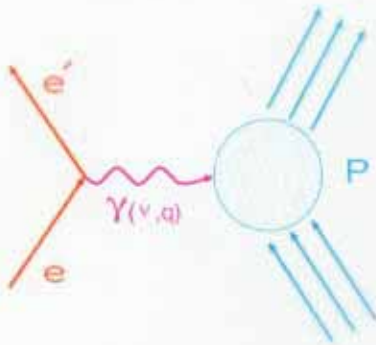
- ▶  $R$  might be small (duality)
- ▶  $R$  might be large (higher twist effects)

Extraction of polarized structure functions from asymmetry measurements.

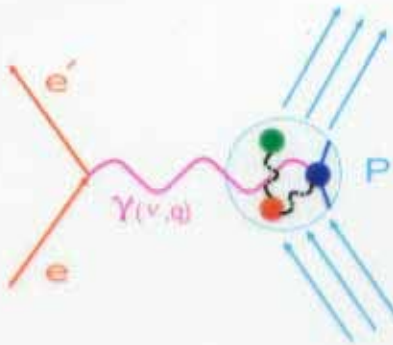
# Unpolarized Electron - Nucleon Scattering

## Single Photon Exchange

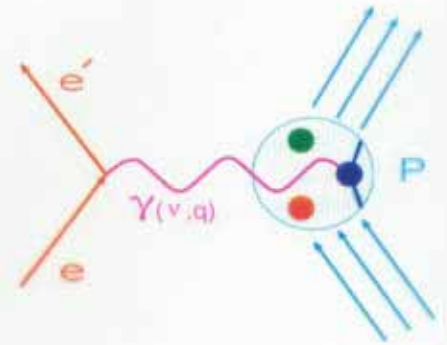
Elastic



Resonance



DIS



In terms of  $\gamma$  coupling:

$$\frac{d\sigma}{d\Omega dE'} = \Gamma [ \sigma_T(x, Q^2) + \epsilon \sigma_L(x, Q^2) ] = \Gamma \sigma_T (1 + \epsilon R)$$

$\Gamma$  : virtual  $\gamma$  flux

$\epsilon$  : virtual  $\gamma$  longitudinal polarization

Alternatively:

$$\frac{d\sigma}{d\Omega dE'} = \Gamma \frac{4\pi^2 \alpha}{x (W^2 - M_N^2)} [ 2x F_1(x, Q^2) + \epsilon F_L(x, Q^2) ]$$

$$(F_L = F_2 \frac{(1 + 4M_N^2 x^2)}{Q^2} - 2xF_1)$$

Experimentally,  $F_2$  Requires a separation of L/T strengths!