

# Study of $\eta$ and $\eta'$ Photoproduction: From Threshold to High Energies

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# Outline

- Our goal:  
an model for  $\eta$  and  $\eta'$  photoproduction from the thresholds to high energies
- $\eta$  **photoproduction**  $\gamma p \rightarrow \eta p$ 
  - $\eta$ -MAID : an isobar model for  $\eta$  photo- and electroproduction  
valid only in resonance regions because of the  $\rho$  and  $\omega$  poles in  $t$ -channel
  - instead, describe  $t$ -channel  $\rho$  and  $\omega$  exchange in terms of **Regge trajectories**  
to comply with correct high energy behavior
  - fit high energy data to determine the  $\rho NN$  and  $\omega NN$  couplings
  - fit data at resonance regions to extract  $N^*$  parameters
- $\eta'$  **photoproduction**  $\gamma p \rightarrow \eta' p$ 
  - use the same  $\rho NN$  and  $\omega NN$  couplings fixed from  $\eta$  photoproduction fit
  - describe  $\eta'$  photoproduction data and study  $N^*$  contributions

# Recent $\eta$ Photoproduction Data

## Cross sections

- TAPS, MAMI in Mainz  
*Krusche et al., Phys. Lett. B358, 40 (1995)* — TAPS '95
- GRAAL, ESRF in Grenoble  
*Renard et al., Phys. Lett. B528, 215 (2002)* — GRAAL '02  
*Rebreyend's talk in N\*2002* — GRAAL prel.
- CLAS, Jefferson Lab  
*Dugger et al., to appear in Phys. Rev. Lett. (2002)* — CLAS '02

## Beam asymmetry

- GRAAL, ESRF in Grenoble  
*Ajaka et al., Phys. Rev. Lett. 81, 1797 (1998)* — GRAAL '98  
*Rebreyend's talk in N\*2002* — GRAAL prel.

## Target asymmetry

- PHOENICS, ELSA in Bonn  
*Bock et al., Phys. Rev. Lett. 81, 534 (1998)* — Bonn '98

More data are coming from CLAS, GRAAL, and CB-ELSA

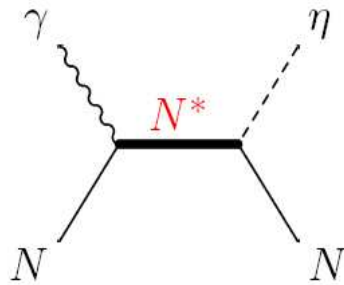
# $\eta$ -MAID

<http://www.kph.uni-mainz.de/MAID>

This isobar model consists of

- Resonance contributions
- Background
  - Born terms
  - Vector meson exchanges

## Resonances



## Breit-Wigner form

$$\begin{pmatrix} E_{\ell\pm} \\ M_{\ell\pm} \end{pmatrix} = \begin{pmatrix} \tilde{E}_{\ell\pm} \\ \tilde{M}_{\ell\pm} \end{pmatrix} f_{\gamma N}(W) \frac{\Gamma_{tot} W_R}{W_R^2 - W^2 - iW_R \Gamma_{tot}} f_{\eta N}(W) C_{\eta N}$$

$$\text{isospin factor } C_{\eta N} = -1$$

$$f_{\eta N}(W) = \left[ \frac{1}{(2j+1)\pi} \frac{k}{|q|} \frac{m_N \Gamma_{\eta N}}{W_R \Gamma_{tot}^2} \right]^{1/2}$$

$$\Gamma_{\eta N} = \beta_{\eta N} \Gamma_R \left( \frac{|q|}{|q_R|} \right)^{2\ell+1} \left( \frac{X^2 + q_R^2}{X^2 + q^2} \right)^\ell \frac{W_R}{W}$$

$$\Gamma_{tot} = \Gamma_{\eta N} + \Gamma_{\pi N} + \Gamma_{\pi\pi N}$$

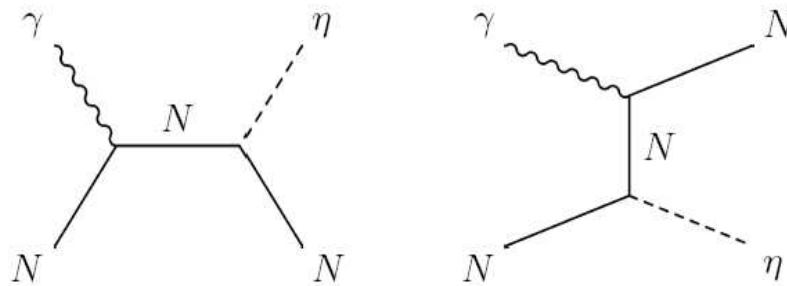
$$f_{\gamma N}(W) = 1$$

## Background

- Born terms
- Vector meson exchanges

The amplitudes of background contributions are obtained by evaluating lowest-order Feynman diagrams using effective Lagrangians

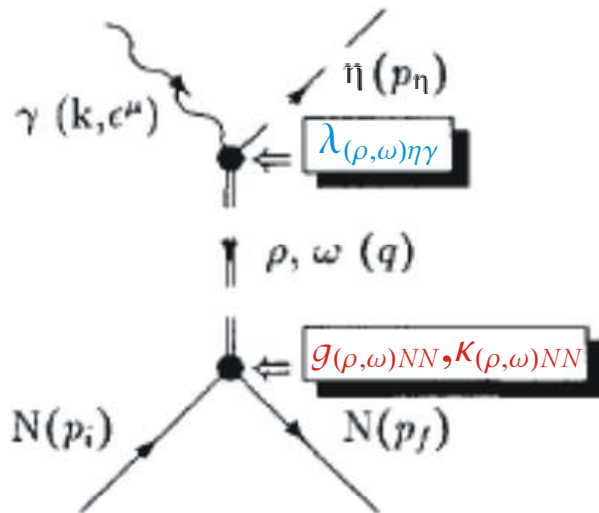
## Born Terms



$$\mathcal{L}_{\gamma NN} = -e\bar{\psi} \left[ \gamma_\mu A^\mu F_1(Q^2) + \frac{\sigma_{\mu\nu}}{2m_N} \partial^\mu A^\nu F_2(Q^2) \right] \psi$$

$$\mathcal{L}_{\eta NN} = -i g_{\eta NN} \bar{\psi} \gamma_5 \psi \phi_\eta$$

## Vector Meson Exchanges



$$\mathcal{L}_{VNN} = g_{VNN} \bar{\psi} \left( \gamma_\mu + \frac{\kappa_{VNN}}{2 m_N} \sigma_{\mu\nu} \partial^\nu \right) V^\mu \psi$$

$$\mathcal{L}_{V\eta\gamma} = \frac{e\lambda_{V\eta\gamma}}{m_\eta} \varepsilon_{\mu\nu\rho\sigma} (\partial^\mu A^\nu) \phi_\eta (\partial^\rho V^\sigma)$$

$$\Gamma_{V \rightarrow \eta\gamma} = \frac{\alpha (M_V^2 - M_\eta^2)^3}{24 M_V^3 M_\eta^2} \lambda_{V\eta\gamma}^2$$

vector meson propagator  $\mathcal{P}_{pole}^V = \frac{1}{t - m_V^2}$

hadronic form factor  $F_V(t) = \left( \frac{\Lambda_V^2 - m_V^2}{\Lambda_V^2 - t} \right)^2$

This description for vector meson exchanges

- works fine in resonance regions ( $W < 2 \text{ GeV}$ )
- but **cannot** extend to high energies

# Regge Trajectory Exchanges

At **high  $s$**  and **low  $t$** , it is known that meson photoproduction can be well described by Regge trajectories in the  $t$ -channel.

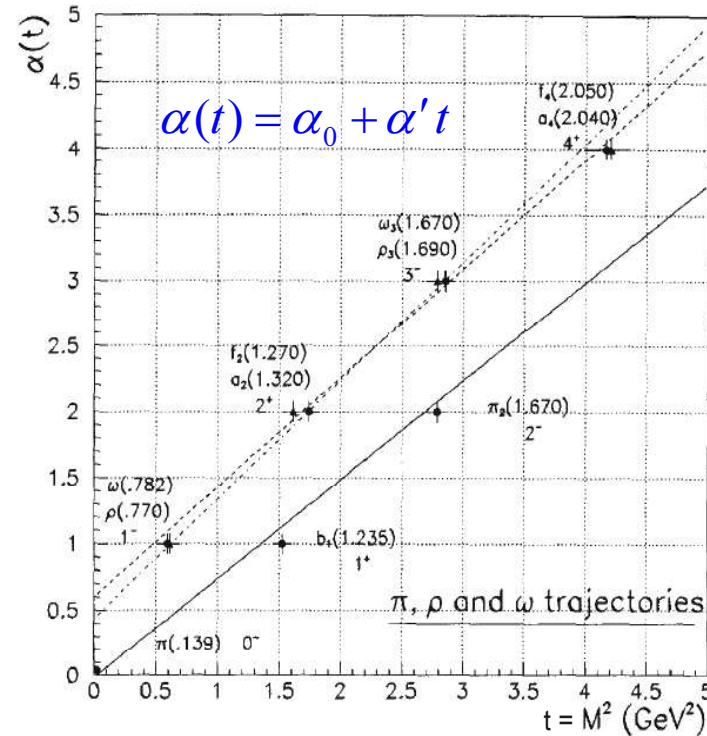
Replace **pole-like propagator**

$$\mathcal{P}_{\text{pole}}^V = \frac{1}{t - m_V^2}$$

With **Regge propagator**

$$\mathcal{P}_{\text{Regge}}^V = \left( \frac{s}{s_0} \right)^{\alpha_V(t)-1} \frac{\pi \alpha'_V}{\sin(\alpha_V(t))} \frac{\mathcal{S}_V + e^{-i\pi\alpha_V(t)}}{2} \frac{1}{\Gamma(\alpha_V(t))}$$

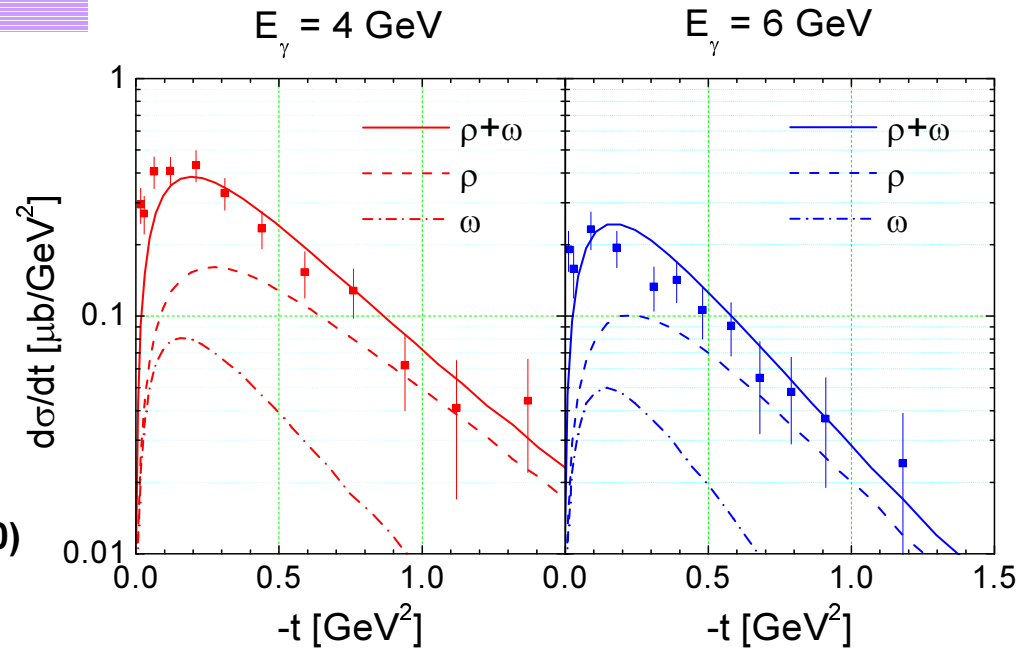
The idea is to economically take into account the exchanges of high-spin particles in the  $t$ -channel which cannot be neglected at higher energies



# Vector Meson Exchanges in $\gamma p \rightarrow \eta p$

Fit **high- $s$** , **low- $t$**  data to determine the vector meson couplings  $g_{VNN}$  and  $\kappa_{VNN}$

Data from **DESY (1970)**



## Vector meson parameters

$V$	$m_V$	$g_{VNN}$	$\kappa_{VNN}$	$\lambda_{V\eta\gamma}$	$\lambda_{V\eta'\gamma}$	$\alpha_V(t)$
$\rho$	768.5 MeV	2.4	3.7	0.810	1.240	$0.55 + 0.8 t/\text{GeV}^2$
$\omega$	782.6 MeV	9	0	0.291	-0.433	$0.44 + 0.9 t/\text{GeV}^2$



## $\gamma p \rightarrow \eta p$ Results

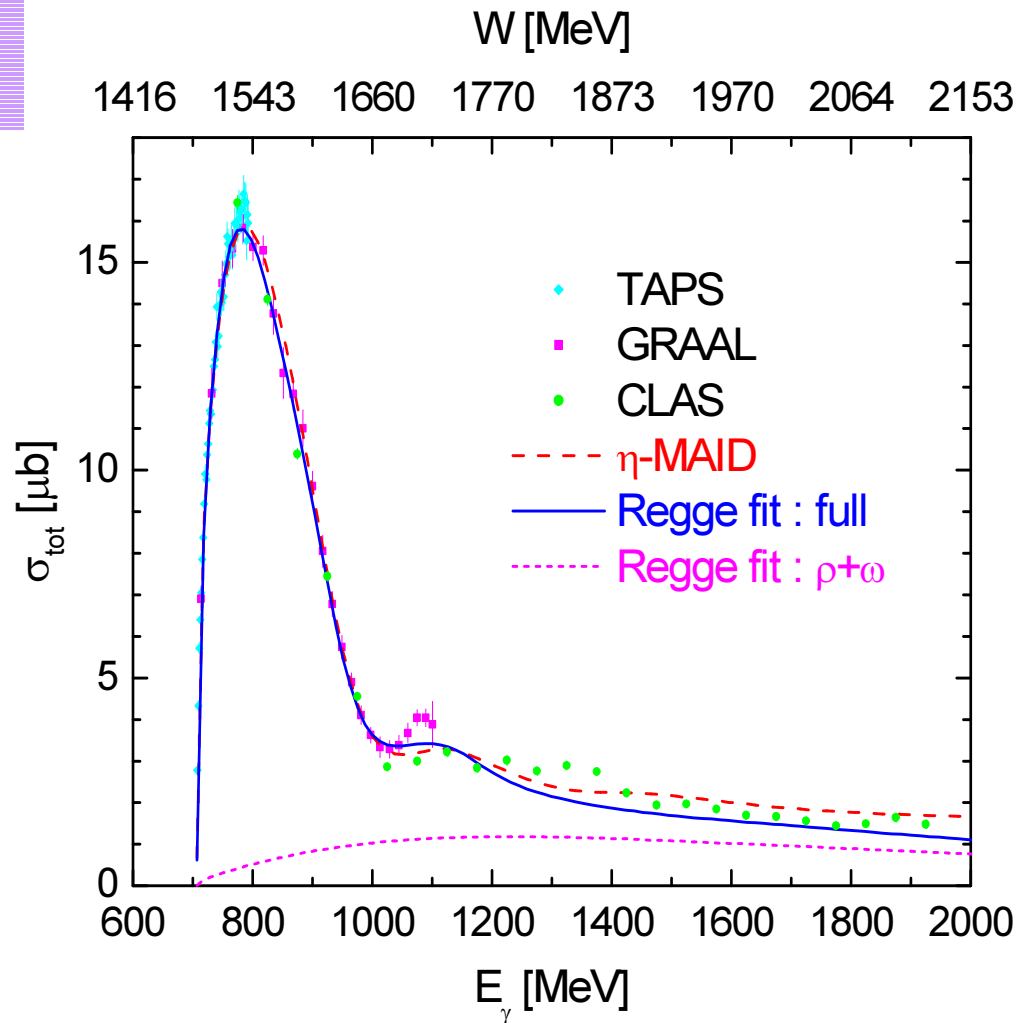
In the following  $\gamma p \rightarrow \eta p$  results shown,

- The  **$\eta$ -MAID** results refers to our isobar model with refitting data which include the recent CLAS cross section data for  $E_\gamma = 0.75$  to  $1.95$  GeV  
M. Dugger, *et al.* (CLAS Collaboration), to appear in PRL
- The **Regge fit** refers to the results from the isobar model with the  $t$ -channel vector meson exchanges described by Regge trajectories

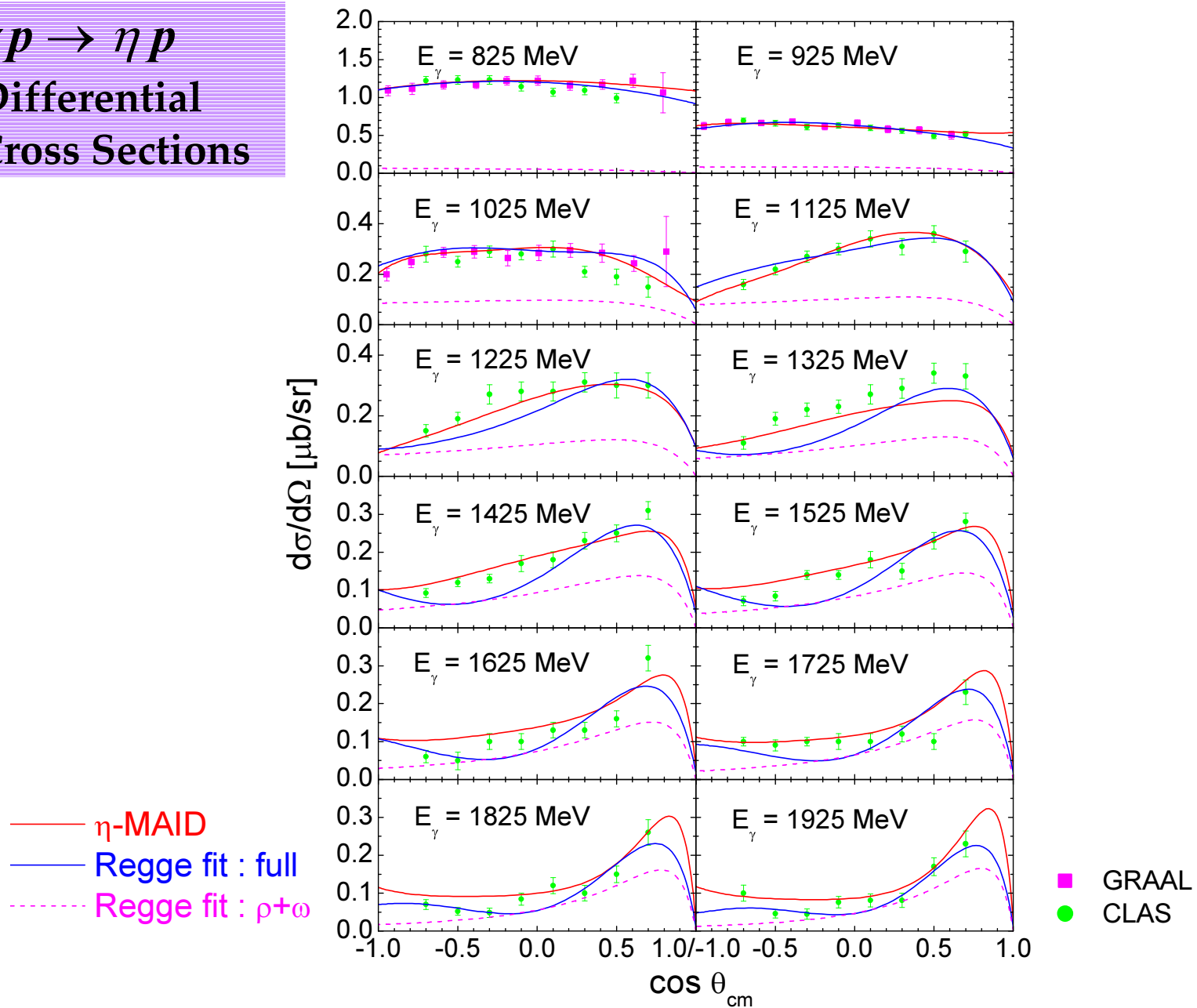
$$\gamma p \rightarrow \eta p$$

## Total Cross Sections

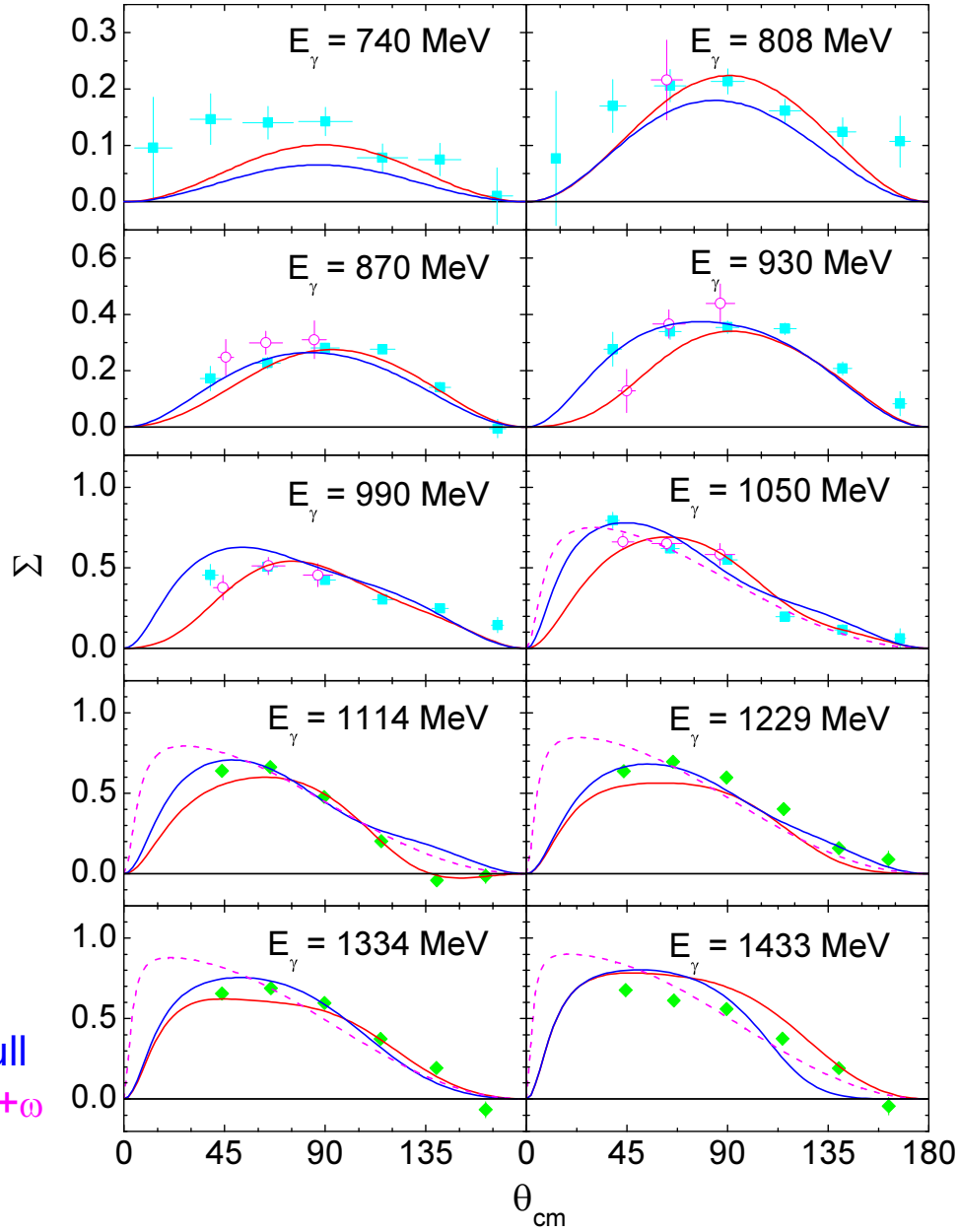
The **GRAAL** and **CLAS** total cross sections are integrated from differential cross section data. Extrapolation to unmeasured angles is required; therefore, they are model dependent quantities.



$\gamma p \rightarrow \eta p$   
 Differential  
 Cross Sections



$\gamma p \rightarrow \eta p$   
**Photon  
 Asymmetry**



—  $\eta$ -MAID  
 — Regge fit : full  
 - - - Regge fit :  $\rho+\omega$

data from **GRAAL**

## Resonance Parameters from $\eta$ -MAID

$N^*$	Mass	Width	$\beta_{\eta N}$	$A^p_{1/2}$	$A^p_{3/2}$
$D_{13}(1520)$	1520	120	0.05%	-39	166
$S_{11}(1535)$	1545	203	50%	125	
$S_{11}(1650)$	1640	130	10%	73	
$D_{15}(1675)$	1682	150	17%	17	24
$F_{15}(1680)$	1670	130	0.04%	-9	145
$D_{13}(1700)$	1700	100	0.7%	-18	-2
$P_{11}(1710)$	1725	100	26%	22	
$P_{13}(1720)$	1720	150	6.6%	18	-19

[MeV]
[ $10^{-3}$  GeV $^{-1/2}$ ]

Numbers in green are fitting parameters

## Resonance Parameters from Regge Fit

$N^*$	Mass	Width	$\beta_{\eta N}$	$A^p_{1/2}$	$A^p_{3/2}$
$D_{13}(1520)$	1520	120	0.02%	-26	166
$S_{11}(1535)$	1530	150	50%	91	
$S_{11}(1650)$	1635	112	12%	53	
$D_{15}(1675)$	1665	150	2%	11	24
$F_{15}(1680)$	1680	130	0.06%	-21	121
$D_{13}(1700)$	1700	100	4.6%	-18	-2
$P_{11}(1710)$	1740	100	12%	31	
$P_{13}(1720)$	1720	150	0.2%	18	-19

[MeV]
[ $10^{-3}$  GeV $^{-1/2}$ ]

Numbers in green are fitting parameters

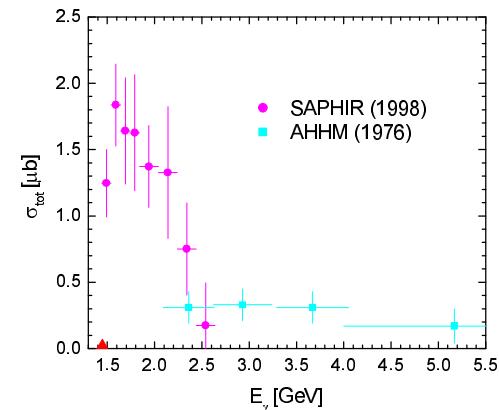
## $\gamma p \rightarrow \eta p$ Summary

- Both models describe current data up to  $E_\gamma = 2$  GeV well, but only the Reggeized model can describe the high energy data
- $N^*$  parameters extracted from two models are different
  - extraction of  $N^*$  parameters depend on the **background**
  - some of these  $N^*$  are insensitive to current  $\eta$  photoproduction data
  - $\Gamma_0, \beta_{\eta N}, A_{1/2,3/2}$  are highly correlated
  - need to compare with other channels or multichannel analysis
- Preliminary GRAAL  $d\sigma/d\Omega$  data (Rebreyend's talk) suggest no dropping in forward angles — something new ?

## $\eta'$ photoproduction



- Use the Regge trajectories in the  $t$ -channel vector meson exchanges with  $g_{VNN}$  and  $k_{VNN}$  fixed from  $\gamma p \rightarrow \eta p$
- Born terms are small; neglected at this moment
- The sharp rise of total cross section near threshold, which is similar to  $\gamma p \rightarrow \eta p$ , suggests a  $S_{11}$  resonance
- Therefore, we start with the minimal set:



**a  $S_{11}$  resonance + Reggeized vector meson exchanges**

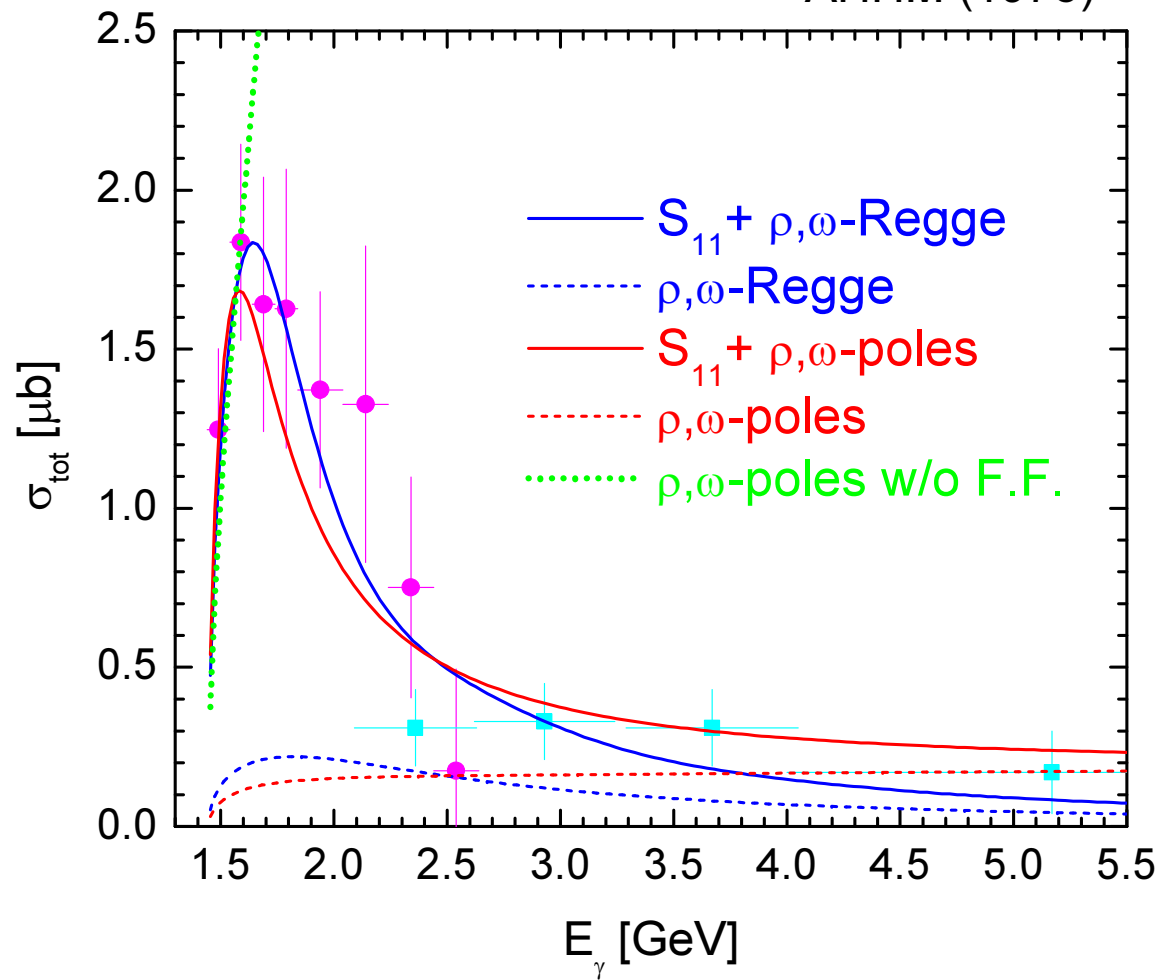


$\gamma p \rightarrow \eta' p$

Total Cross Sections

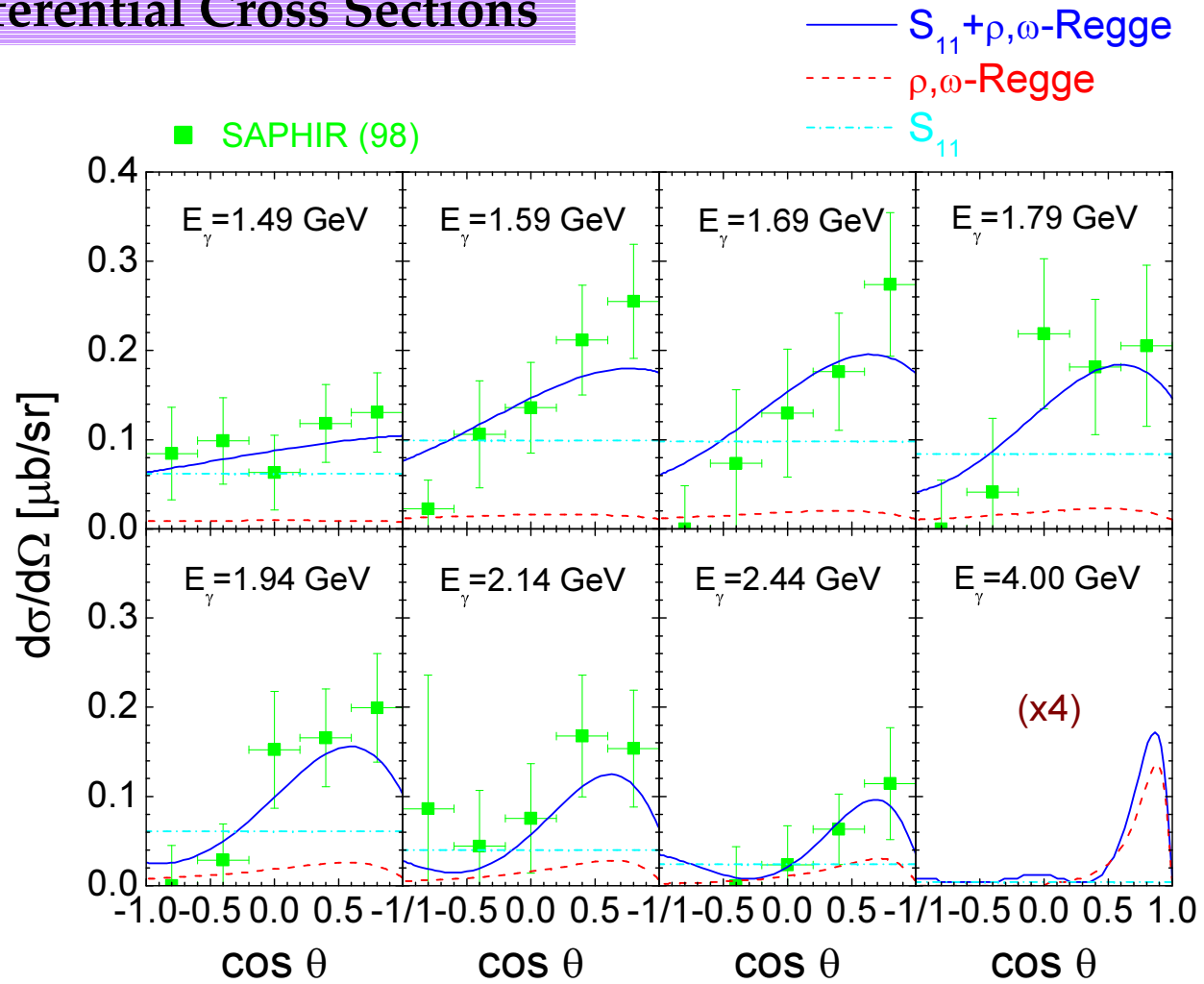
● SAPHIR (1998)

■ AHHM (1976)



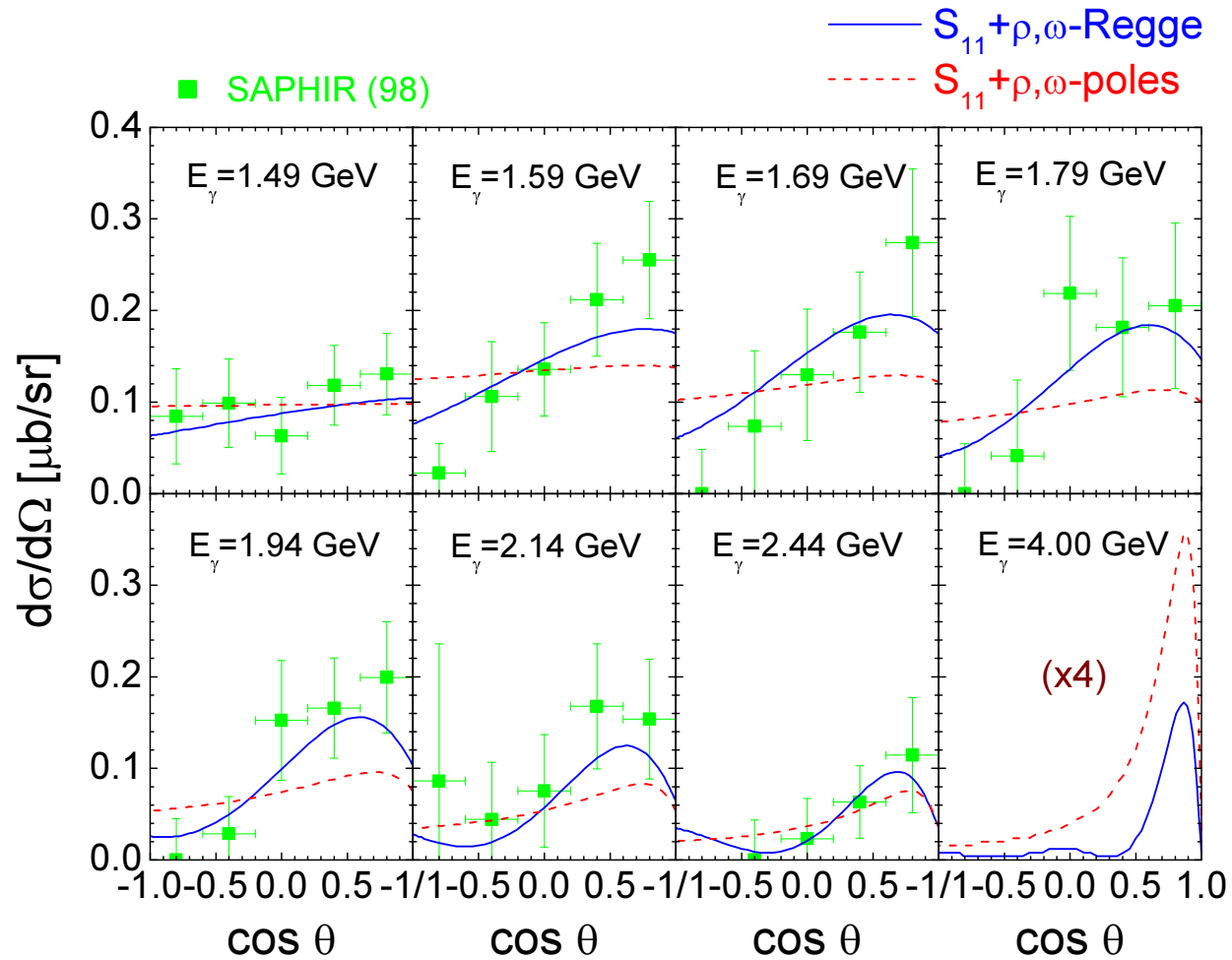
$\gamma p \rightarrow \eta' p$

Differential Cross Sections



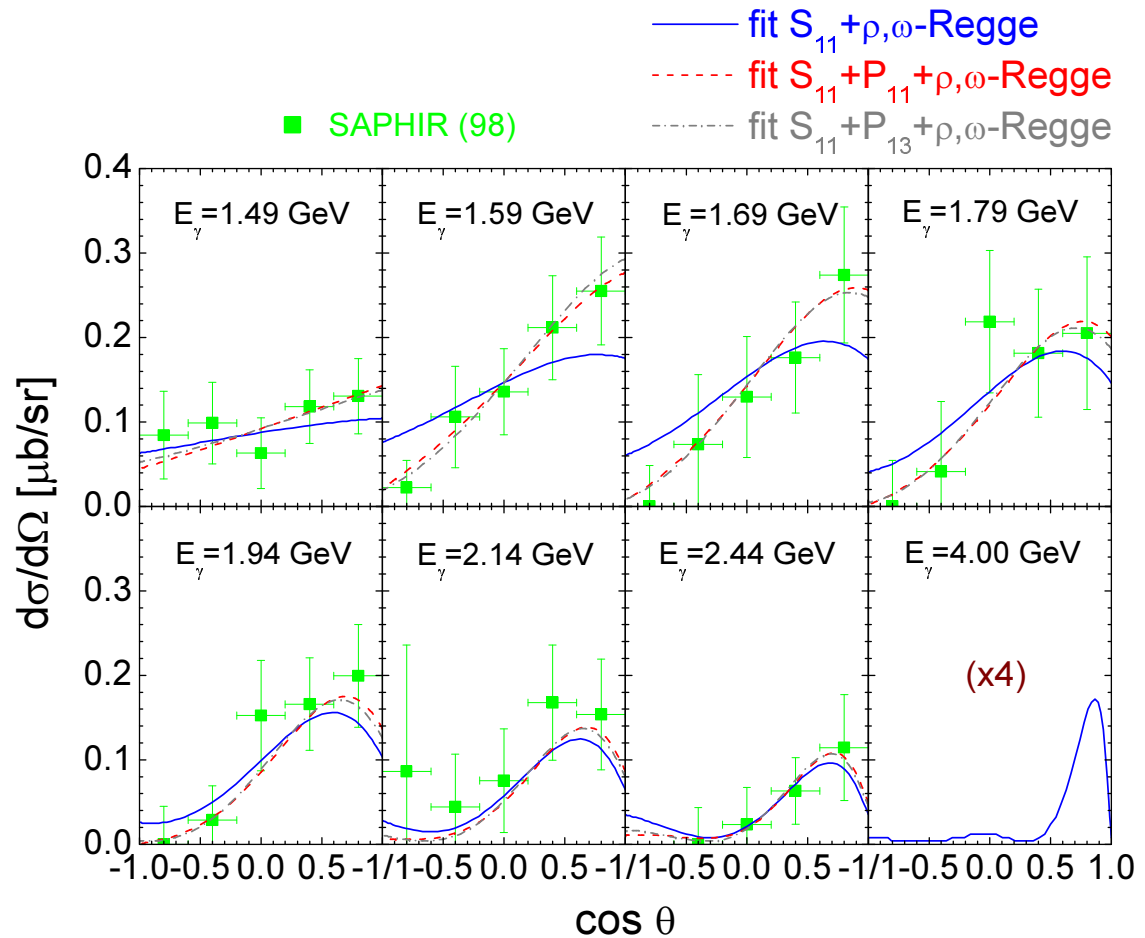
$\gamma p \rightarrow \eta' p$

Differential Cross Sections



# $\gamma p \rightarrow \eta' p$ Differential Cross Sections

An additional  $P_{11}$  or  $P_{13} N^*$  can equally improve the fit.



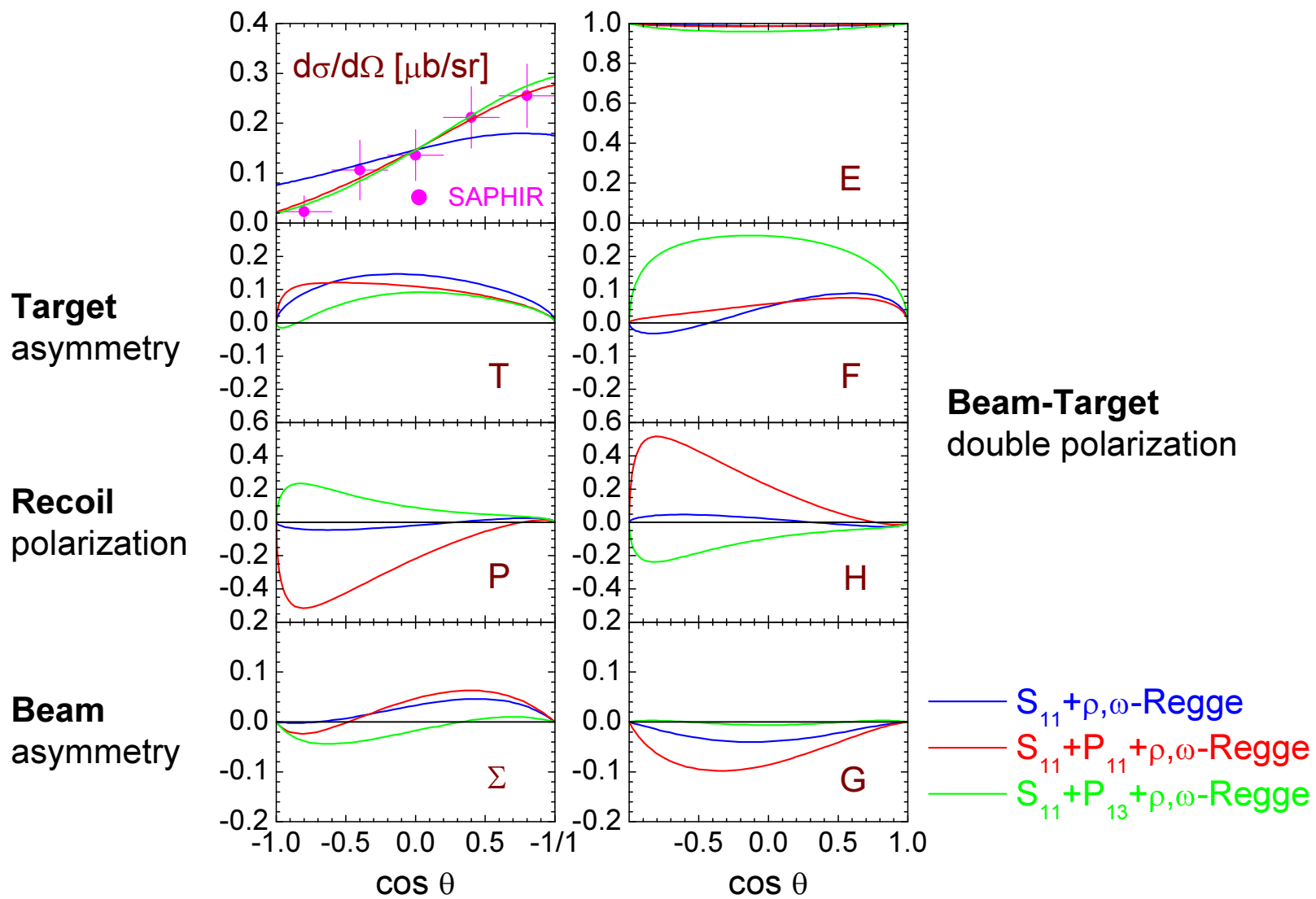
Results:

$S_{11} + \rho, \omega$  fit :  $M_{S_{11}} = (1959 \pm 35) \text{ MeV}$

$S_{11} + P_{11} + \rho, \omega$  fit :  $M_{S_{11}} = (1932 \pm 16) \text{ MeV}$  ,  $M_{P_{11}} = (1951 \pm 32) \text{ MeV}$

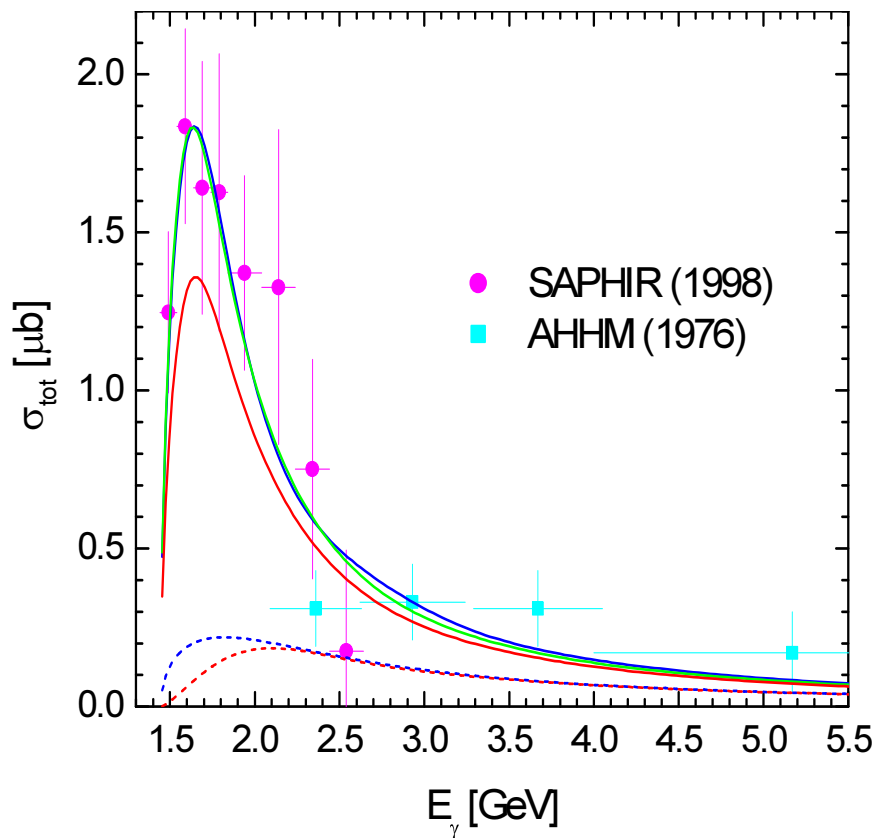
$S_{11} + P_{13} + \rho, \omega$  fit :  $M_{S_{11}} = (1933 \pm 14) \text{ MeV}$  ,  $M_{P_{13}} = (1954 \pm 37) \text{ MeV}$

$\gamma p \rightarrow \eta' p$



# Duality

$s$ -channel resonances  $\leftrightarrow$   $t$ -channel Reggeized vector meson exchanges



There is some amount of **double counting** for  $s$ -wave in the  $S_{11}$  resonance region.

In principle, we should **remove  $s$ -wave** from Reggeized vector meson exchanges in an energy-dependent way.

- $S_{11} + \rho, \omega$ -Regge
- ⋯  $\rho, \omega$ -Regge
- $S_{11} + \rho, \omega$ -Regge (minus  $s$ -wave)
- ⋯  $\rho, \omega$ -Regge (minus  $s$ -wave)
- refit  $S_{11} + \rho, \omega$ -Regge (minus  $s$ -wave)

## $\gamma p \rightarrow \eta' p$ Summary

- Our isobar model modified by Reggeized  $t$ -channel exchanges describe current data reasonably well, even without including  $P$ -wave  $N^*$
- Including either a  $P_{11}$  or a  $P_{13}$   $N^*$  equally improves the fit; need polarization measurements (e.g.  $H$  and  $F$ ) to distinguish their contribution
- It is demonstrated that  $\eta'$  photoproduction is a very good reaction to study  $N^*$  above  $W = 1.9$  GeV, which are rarely studied
- More precise data are needed for  $\gamma p \rightarrow \eta' p$  reaction in order to determine involved  $N^*$   
**Good news** — data coming from [JLab](#), [GRAAL](#), and [Bonn](#)
- Need to understand more about the **duality** problem and how to avoid the **double counting** for  $s$ - and  $t$ -channels when Regge trajectories are used